

1. Find the solution of each of the following recurrence relations and initial conditions
  - (a)  $a_n = 3a_{n-1}$ ,  $a_0 = 2$ .
  - (b)  $a_n = a_{n-1} + 2$ ,  $a_0 = 3$ .
  - (c)  $a_n = 2a_{n-1} - 1$ ,  $a_0 = 1$ .
  - (d)  $a_n = 2na_{n-1}$ ,  $a_0 = 1$ .
2. First-order and second-order linear recursions  
6.11, 6.31, 6.32
3. Consider the nonhomogeneous linear recurrence relation  $a_n = 2a_{n-1} + 2^n$ .
  - (a) Show that  $a_n = n2^n$  is a (particular) solution of this recurrence relation
  - (b) Find all solutions of this recurrence relation.
  - (c) Find the solutions of this recurrence relation with  $a_0 = 2$ .
4. (a) Determine values of the constants  $A$  and  $B$  such that  $a_n = An + B$  is a (particular) solution of recurrence relation  $a_n = 2a_{n-1} + n + 2$ .
  - (b) Find all solution of this recurrence relation.
  - (c) Find the solutions of this recurrence relation with  $a_0 = 4$ .
5. (a) Determine value of the constant  $A$  such that  $a_n = A4^n$  is a (particular) solution of recurrence relation  $a_n = -5a_{n-1} - 6a_{n-2} + 42 \cdot 4^n$ .
  - (b) Find all solution of this recurrence relation.
  - (c) Find the solutions of this recurrence relation with  $a_1 = 56$  and  $a_2 = 278$ .
6. Proof  
6.34