

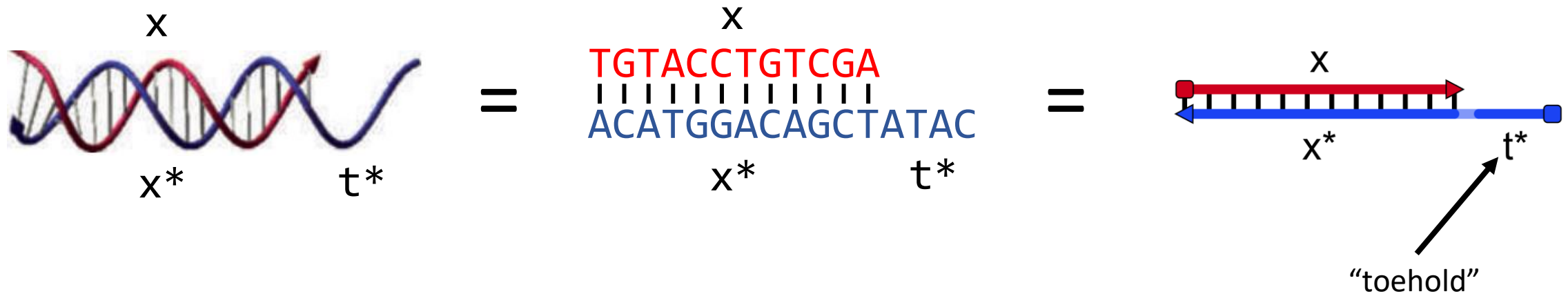
# DNA strand displacement

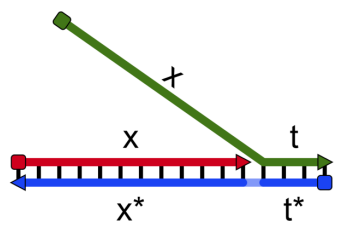
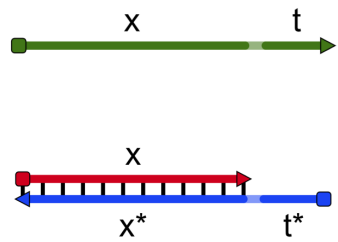
DNA reconfiguring itself without enzymes

slides © 2023, David Doty

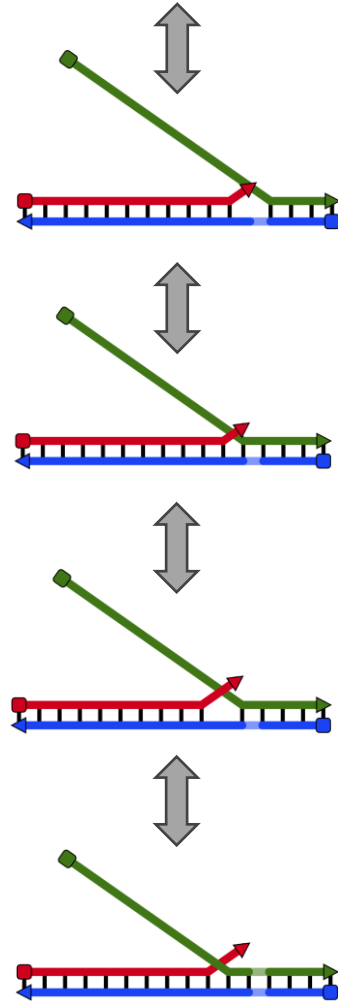
ECS 232: Theory of Molecular Computation, UC Davis

# DNA strands with “long” and “short” (toehold) binding domains

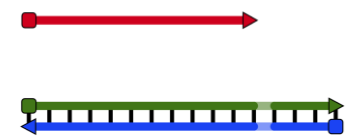




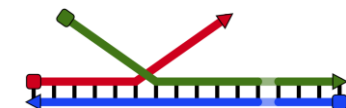
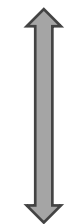
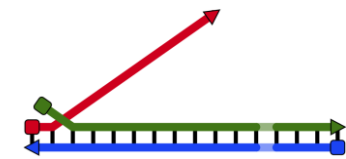
“breathing”/  
“fraying”



# DNA strand displacement example



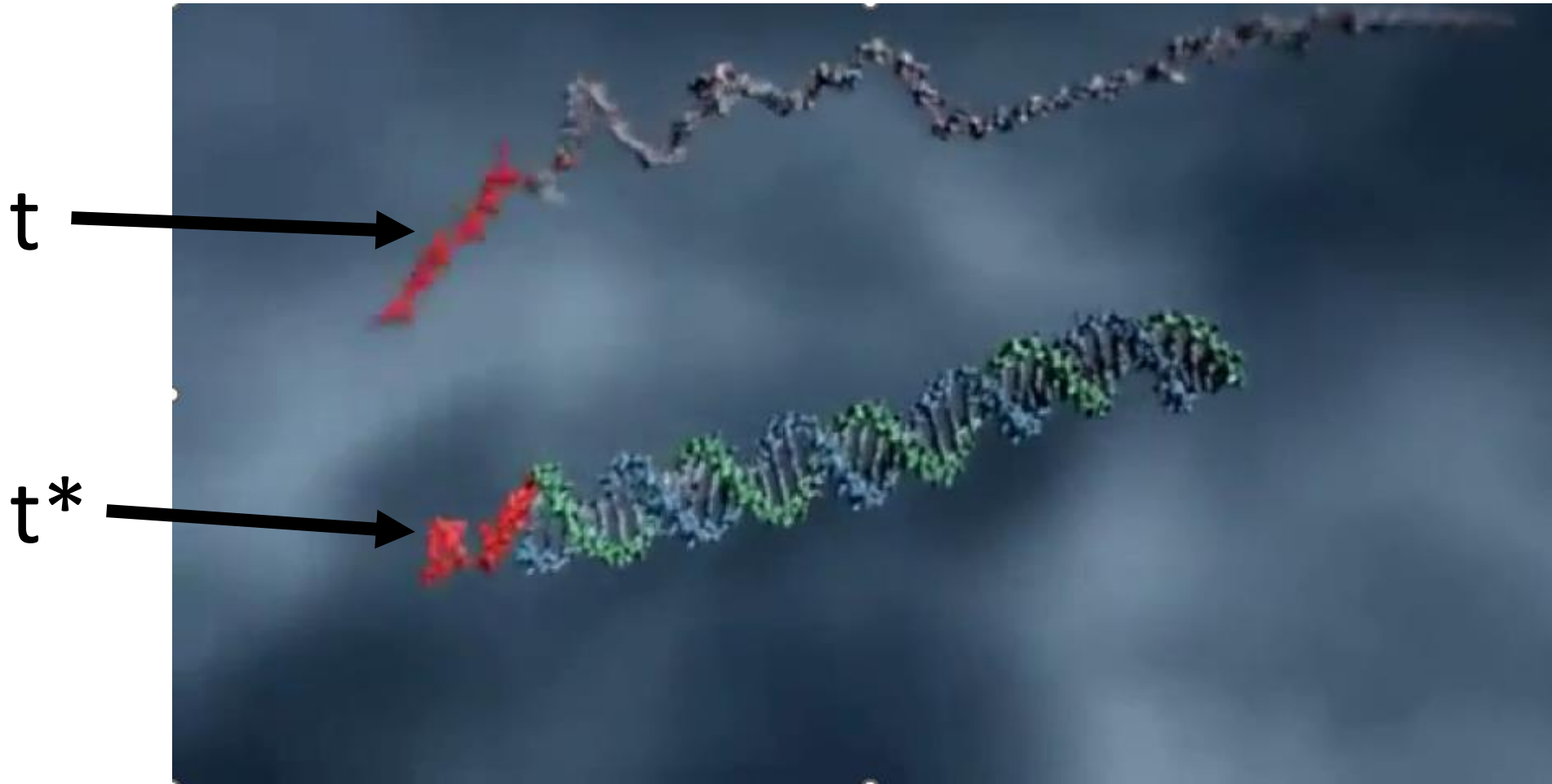
↑ irreversible



branch migration  
←→

# DNA strand displacement

<https://www.microsoft.com/en-us/research/video/dna-strand-displacement/>



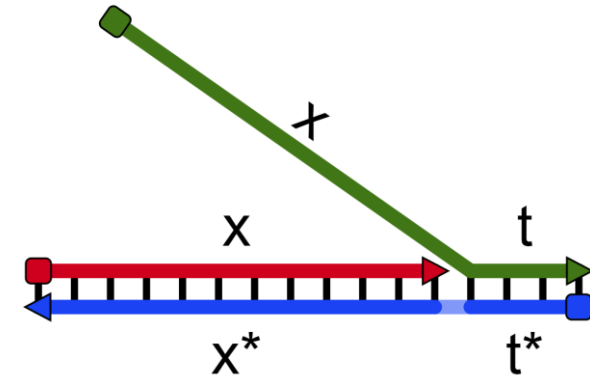
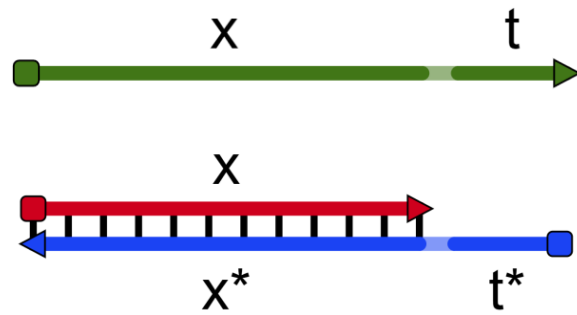
# DNA strand displacement model

3 rules:

1. bind
2. release
3. displace

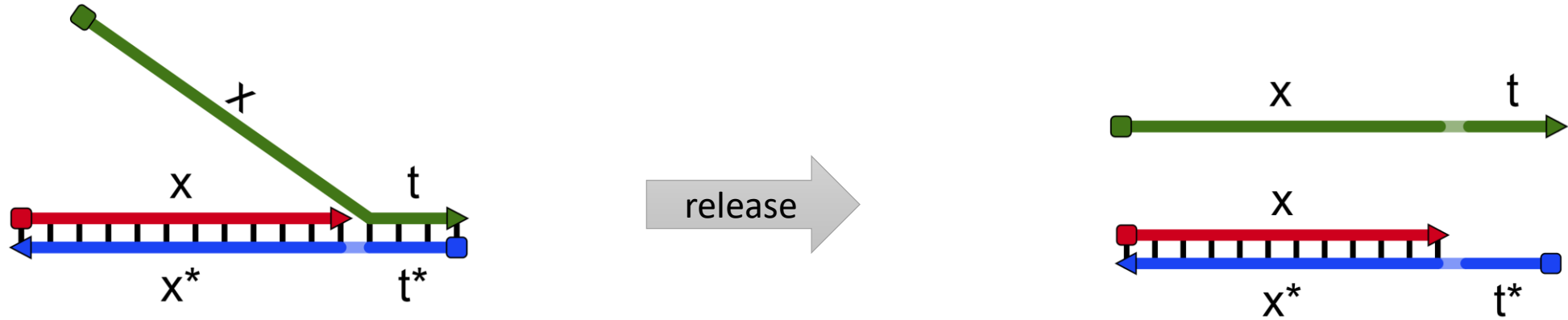
# Bind rule

single-stranded complementary domains can bind



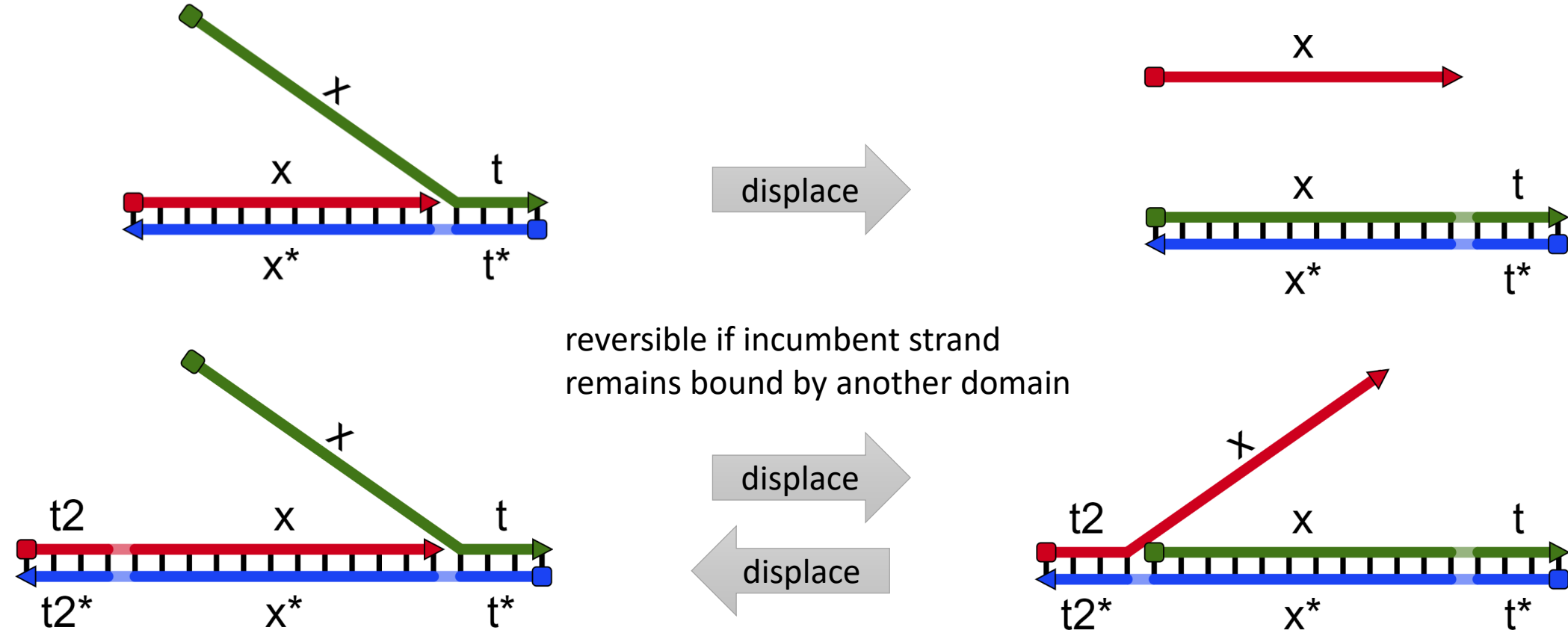
# Release rule

double-stranded complementary domains can unbind  
**IF** they are toehold-length (short,  $< 8$  nt)



# Displace rule

A domain (invader) can displace an identical domain (incumbent) of another strand, **IF** neighboring domains are already bound

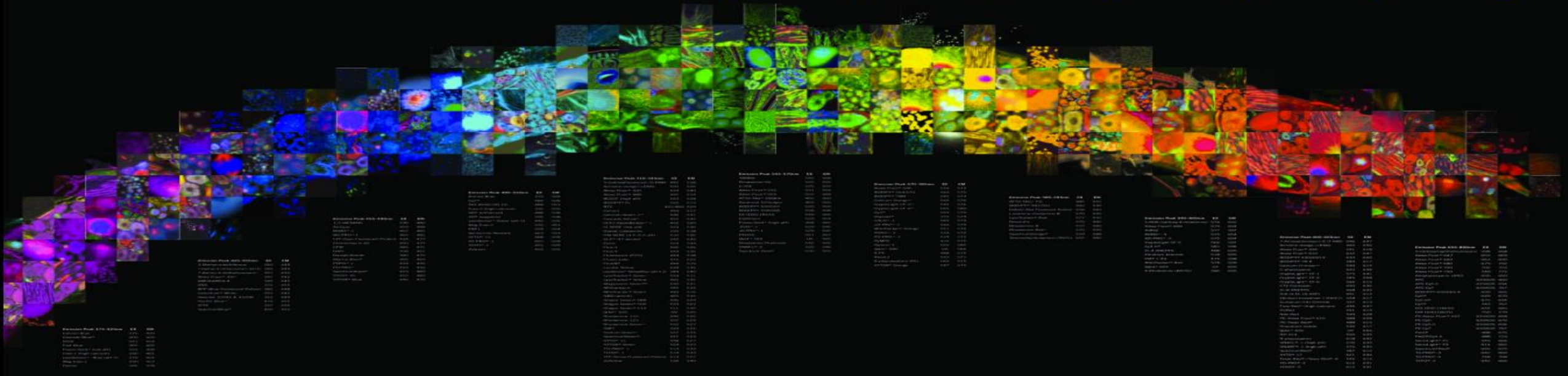




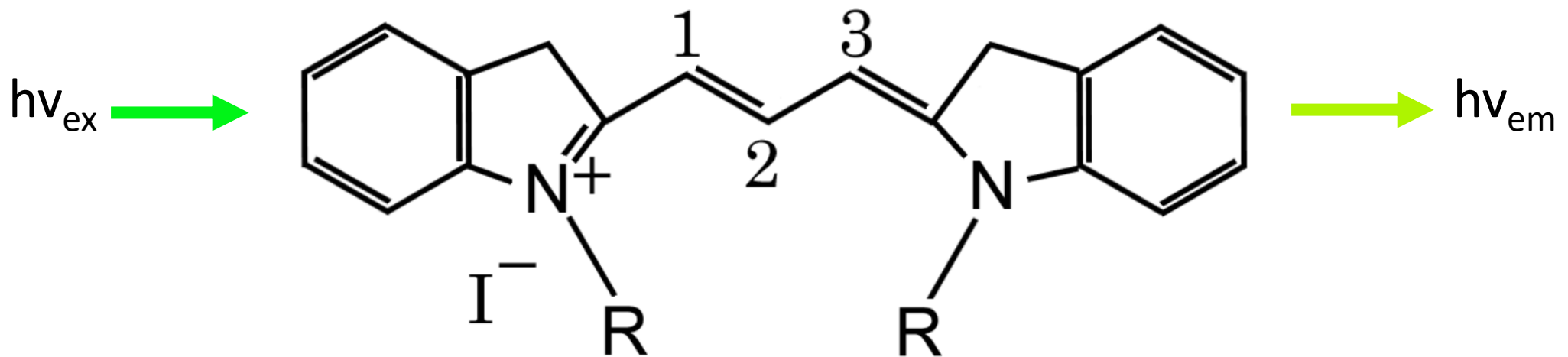
# Readout

How do we read a “signal” in a DNA strand displacement system?

# F L U O R O E S S E N C E



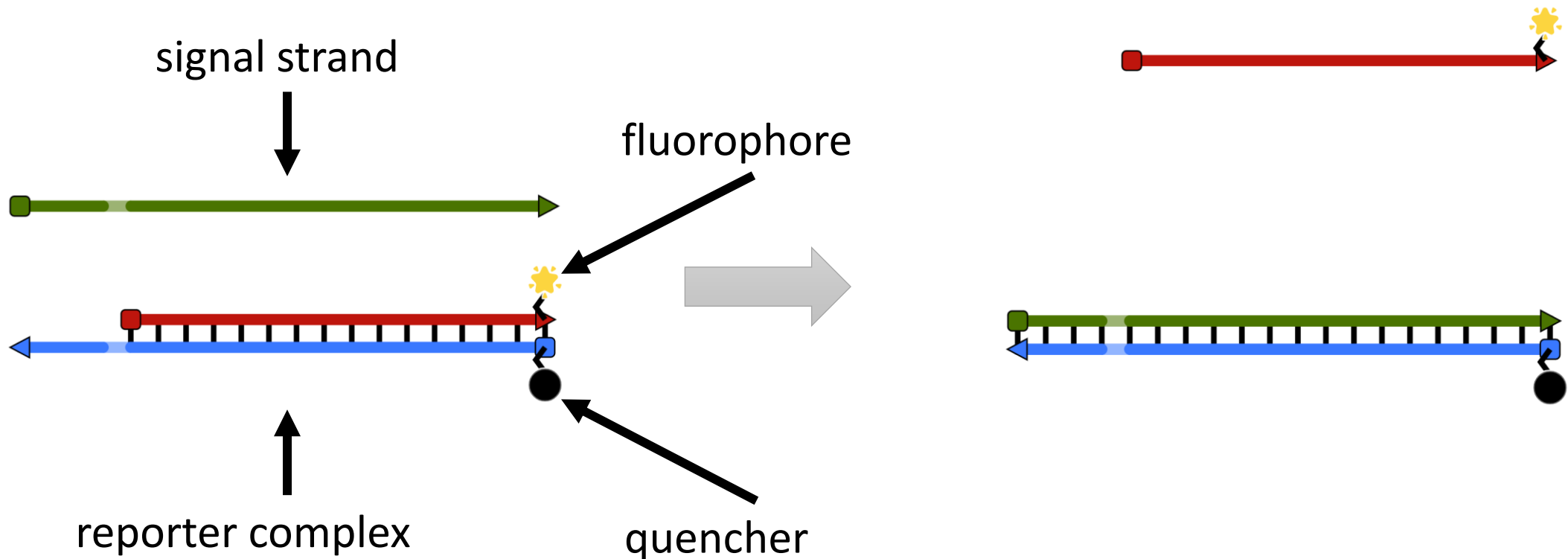
Fluorophores, when “excited” by light at one wavelength, emit light at a longer wavelength.



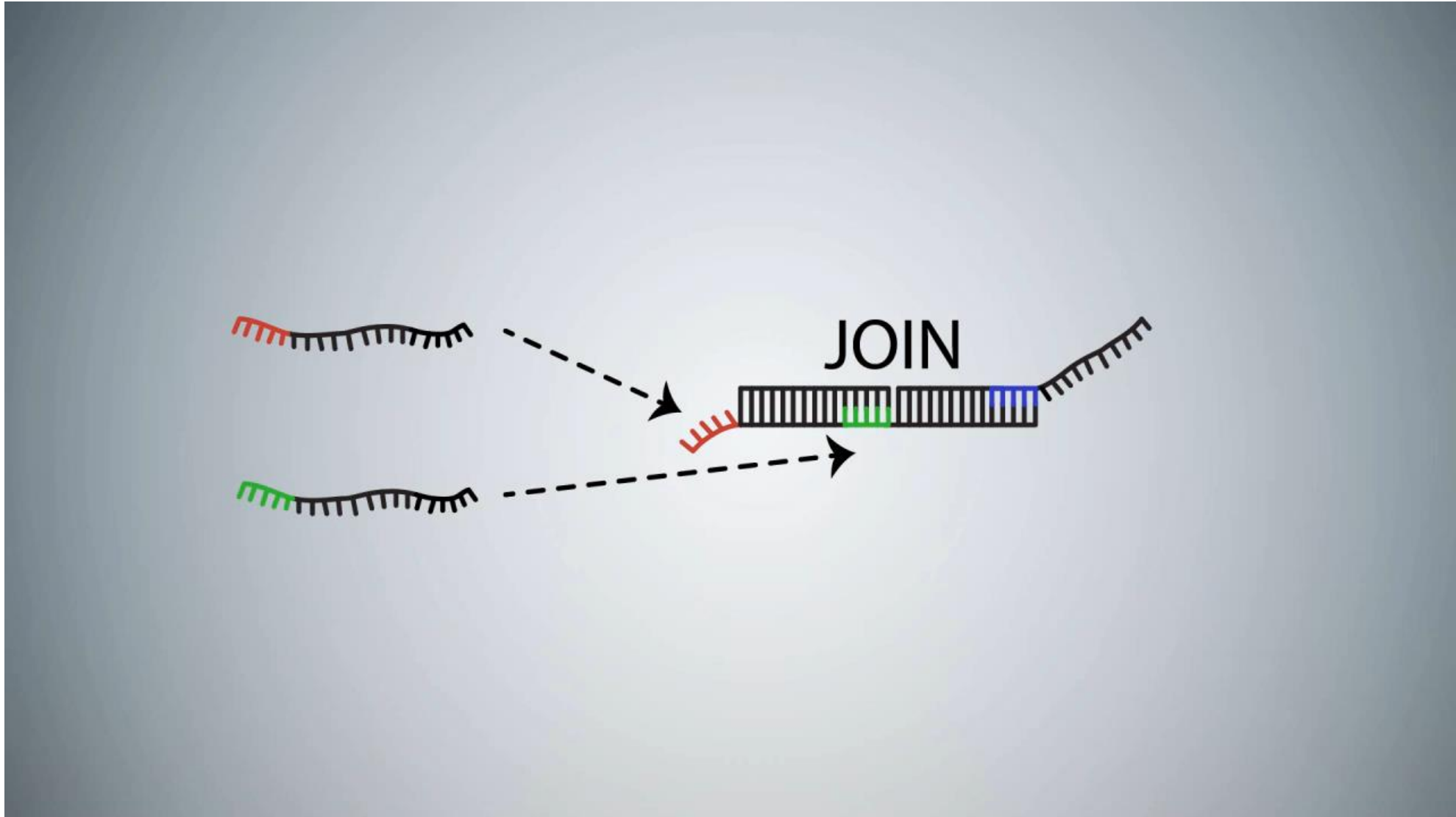
# Reporter complexes

How do we read a “signal”?

“signal” = single strand is freed from a double-stranded complex.



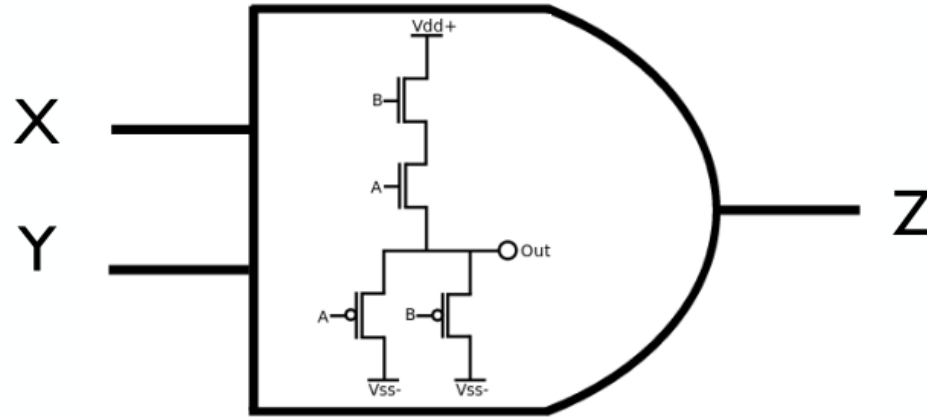
# Reporter complex depiction



# Boolean logic with DNA strand displacement

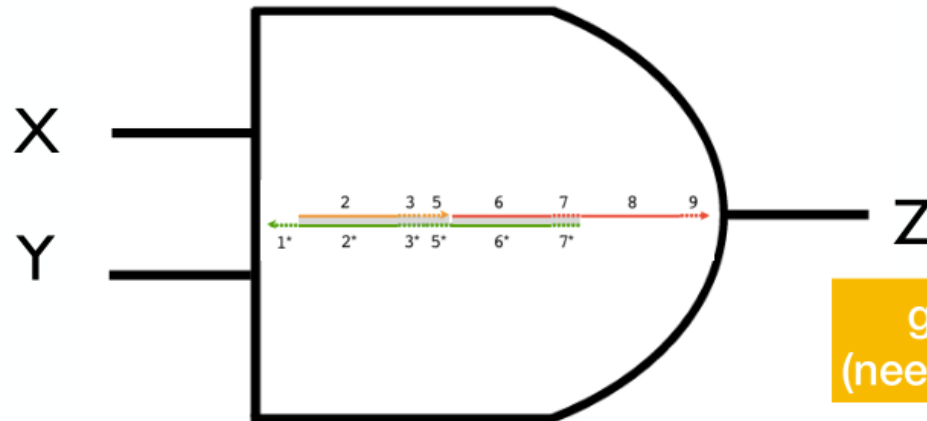
# AND gate

voltages



release Z if and only if X and Y are present

strands

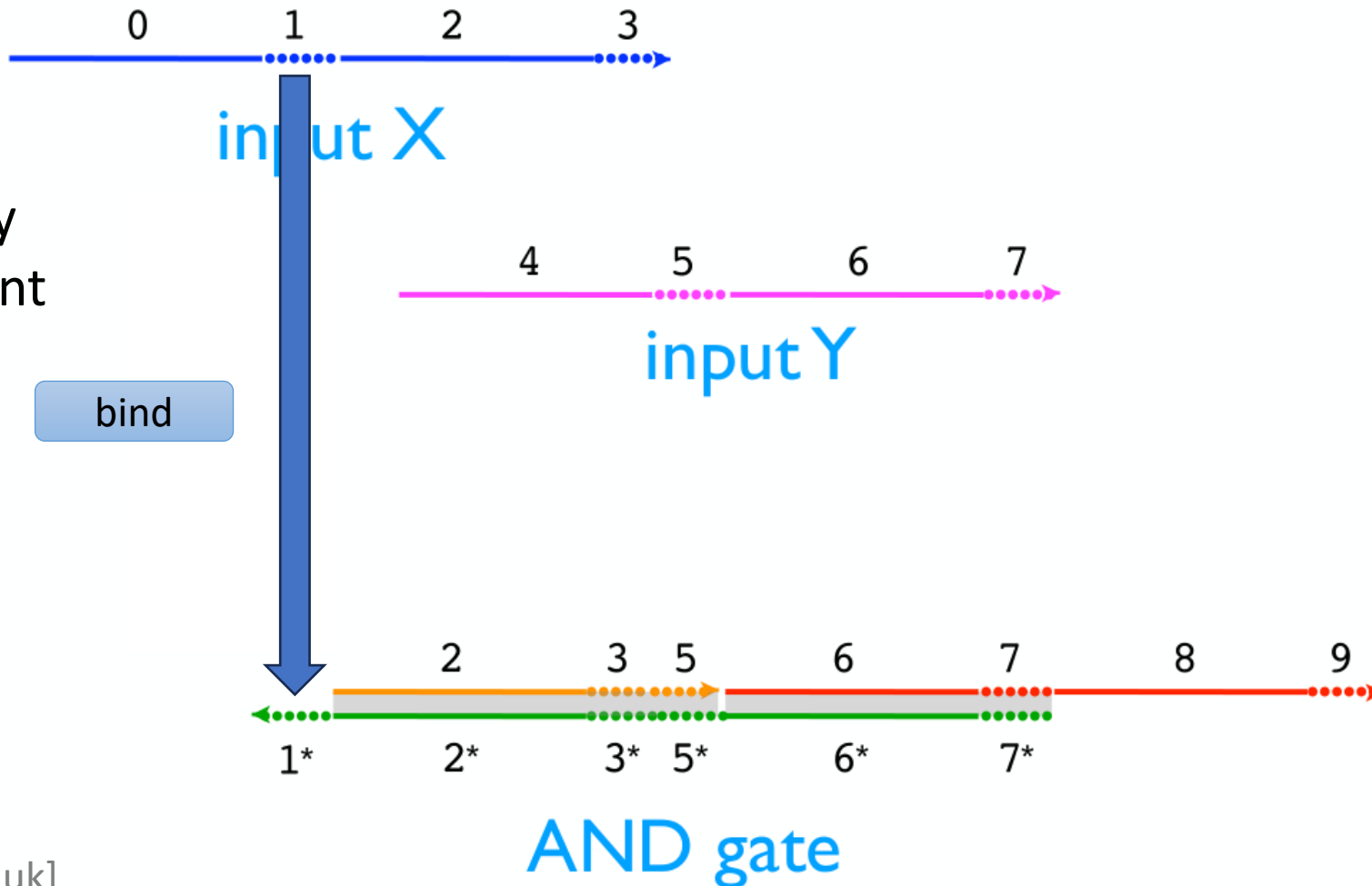


gates get consumed!  
(need to have many copies)

gate=complex

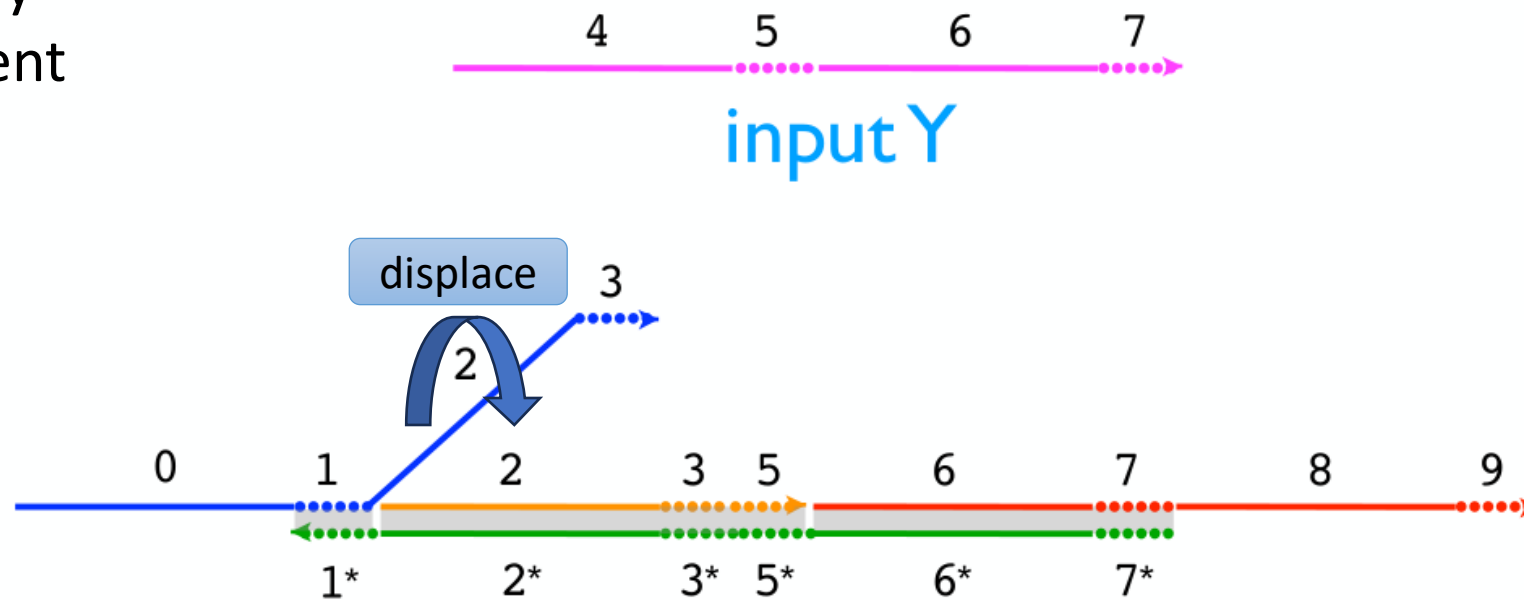
# Strand displacement cascade example: AND gate

release Z if and only  
if X and Y are present



# Strand displacement cascade example: AND gate

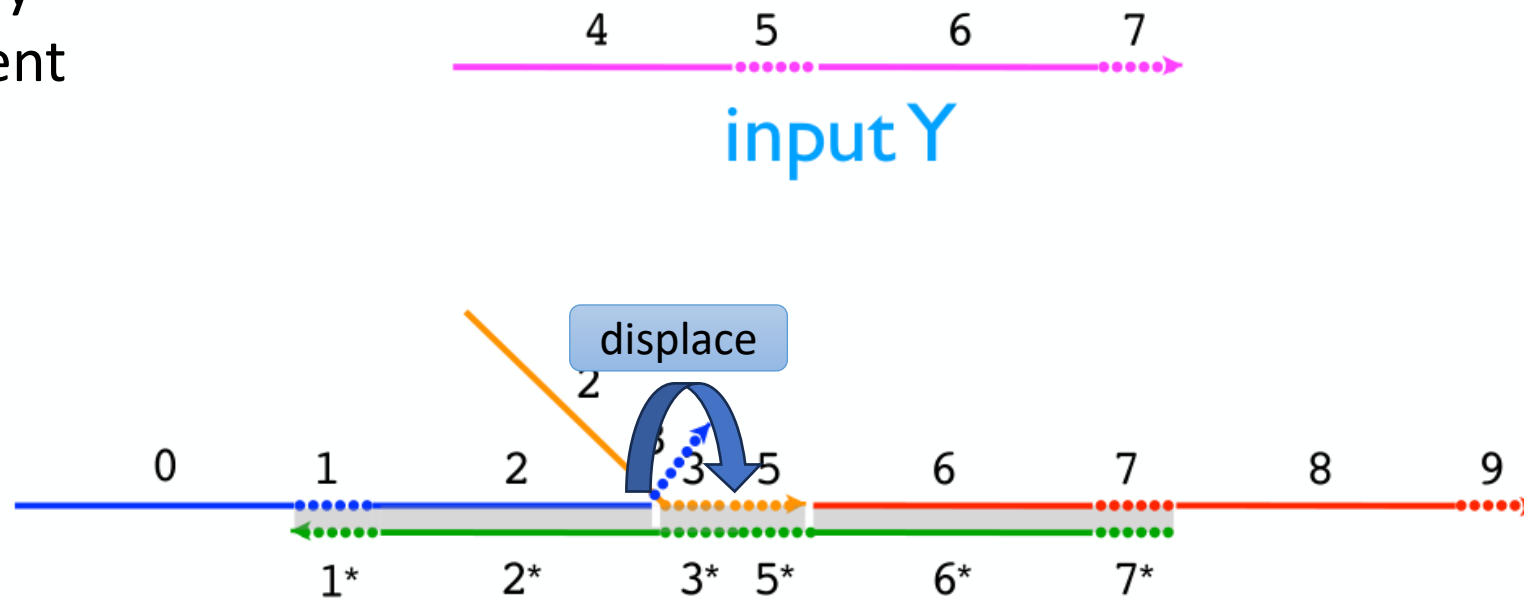
release Z if and only  
if X and Y are present





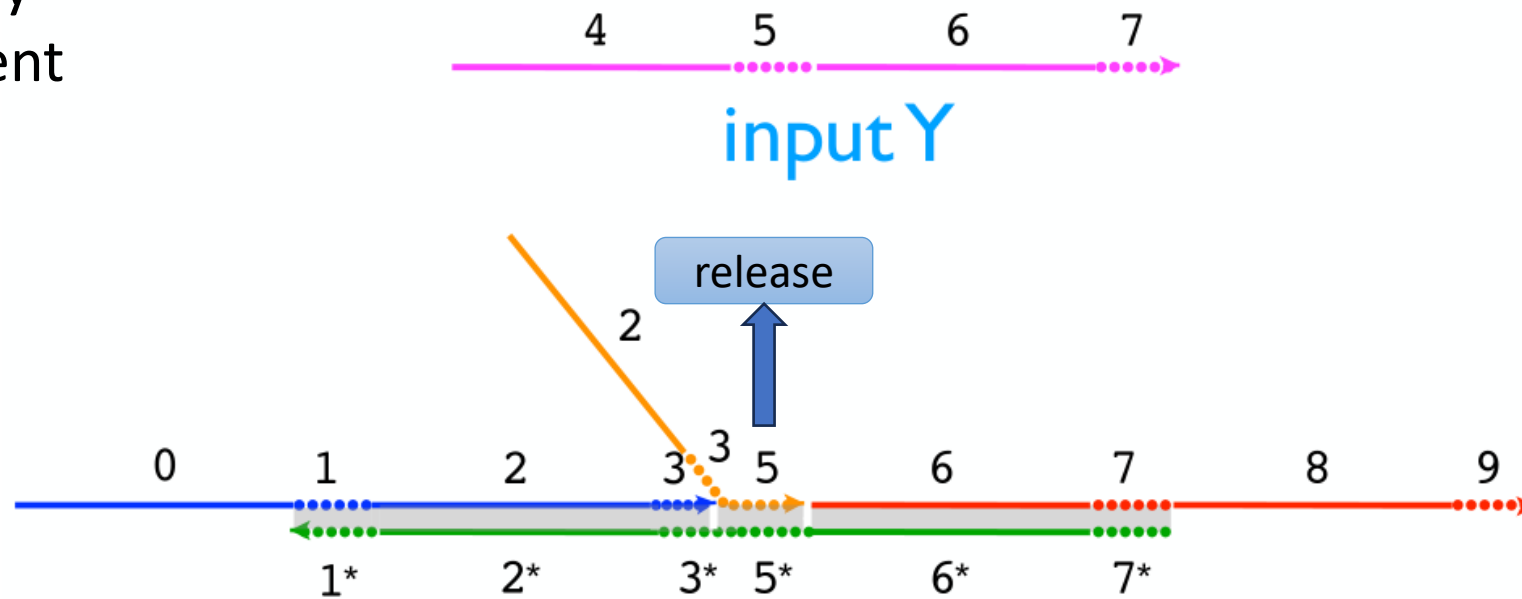
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# Strand displacement cascade example: AND gate

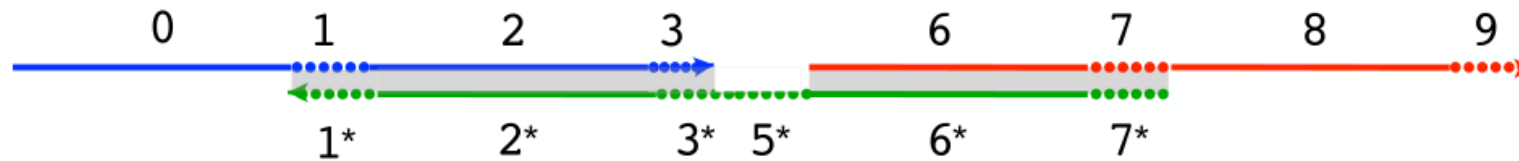
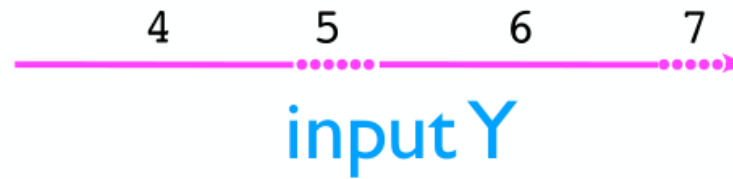
release Z if and only  
if X and Y are present



# Strand displacement cascade example: AND gate



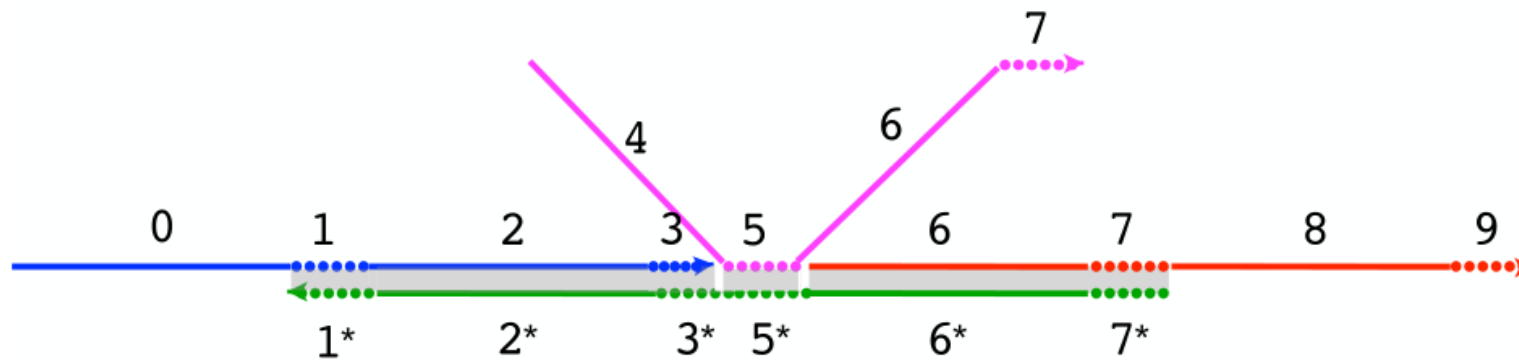
release Z if and only  
if X and Y are present



# Strand displacement cascade example: AND gate



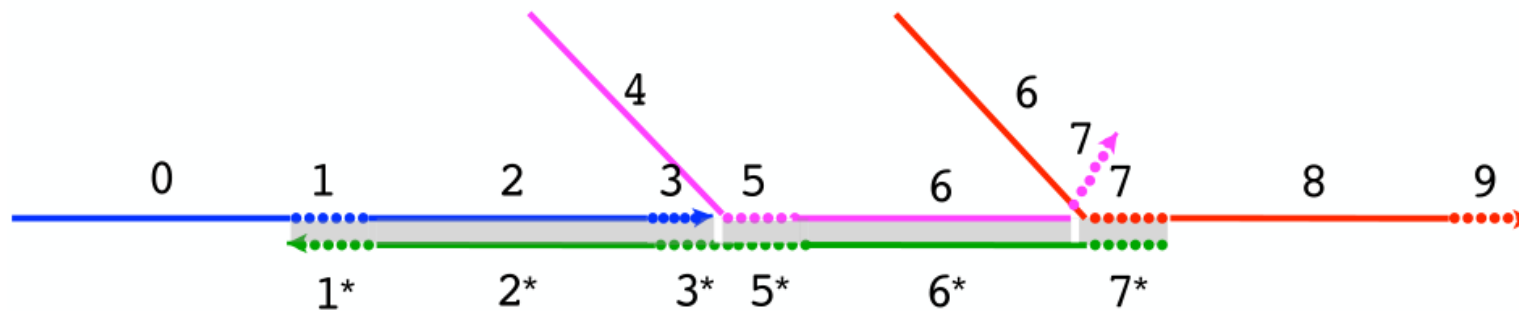
release Z if and only  
if X and Y are present



# Strand displacement cascade example: AND gate



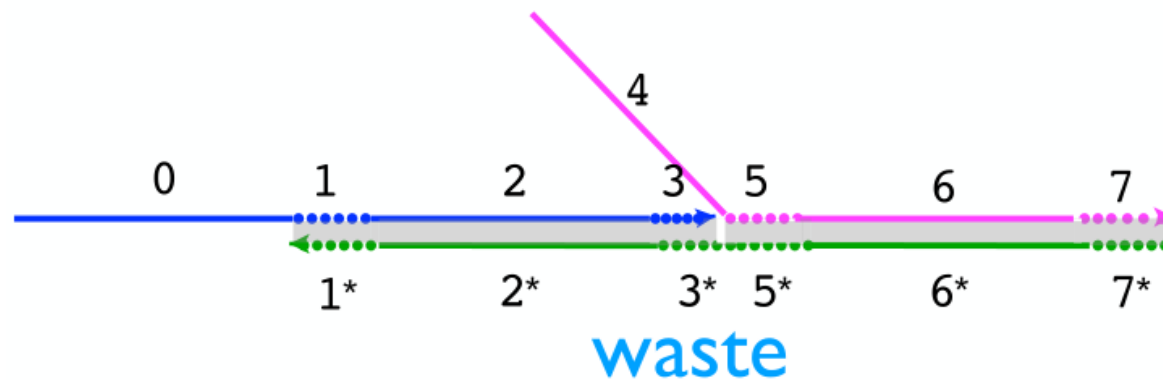
release Z if and only  
if X and Y are present



# Strand displacement cascade example: AND gate

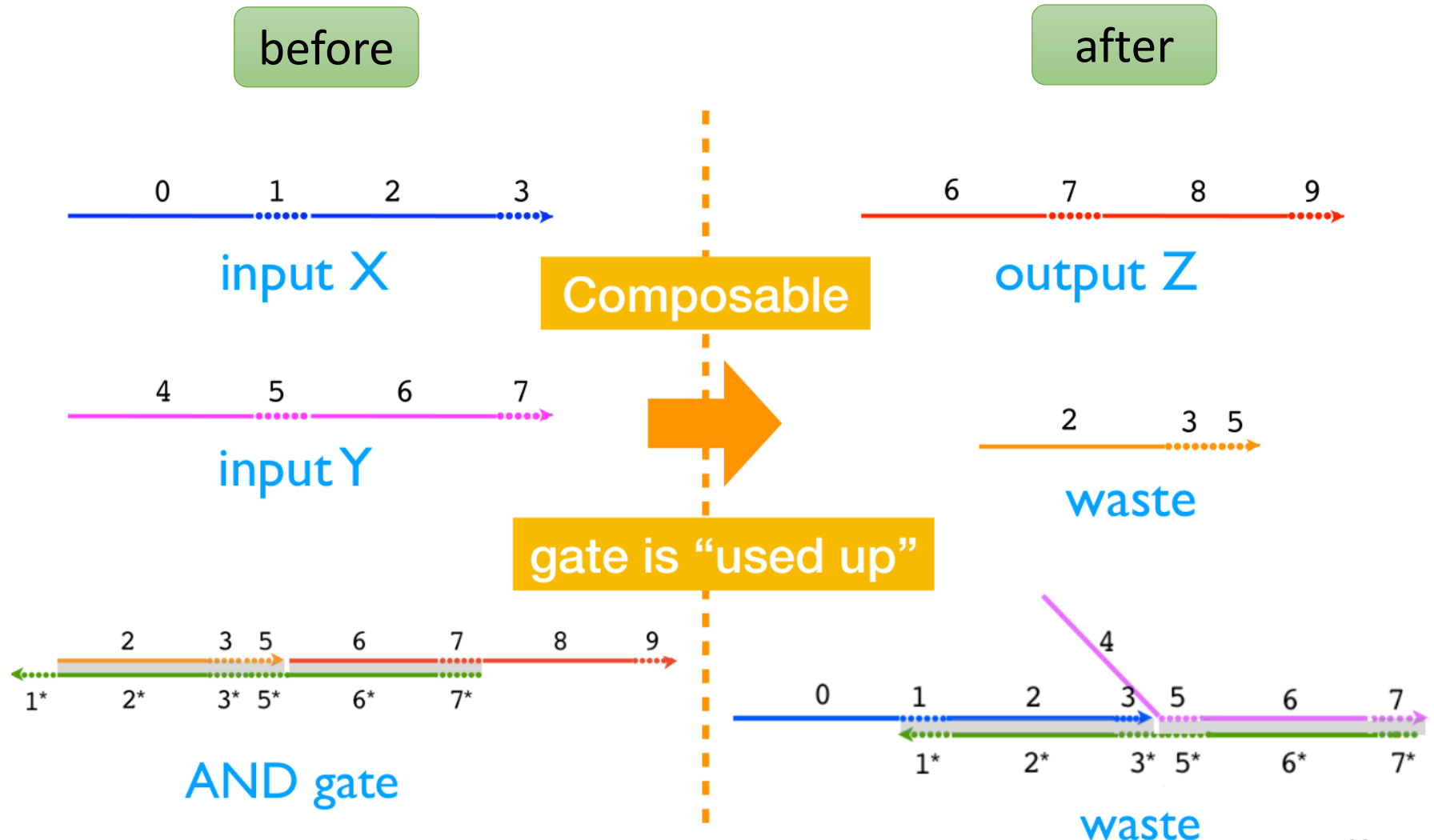


release Z if and only  
if X and Y are present

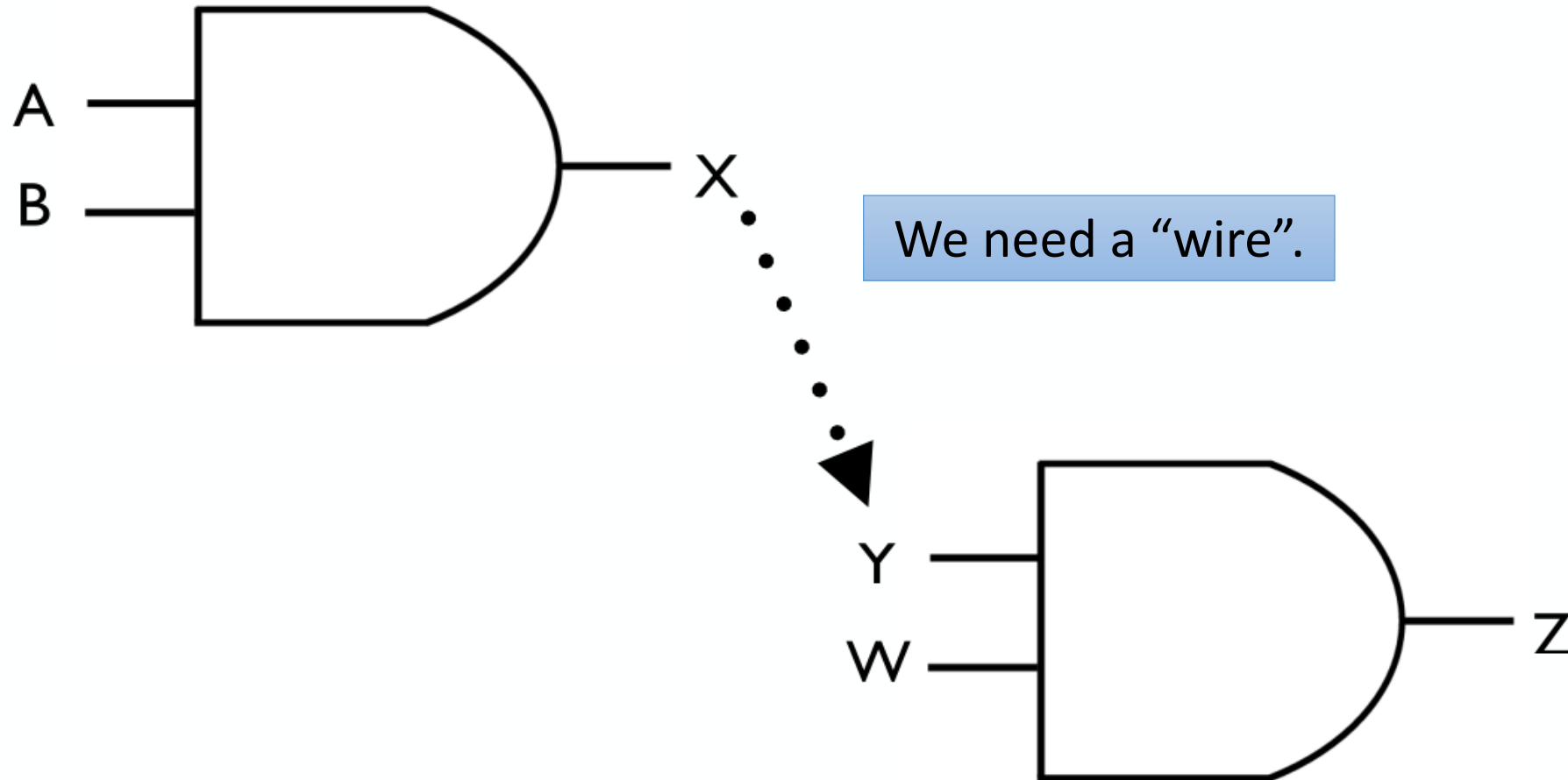


# Strand displacement cascade example: AND gate

release Z if and only if X and Y are present



# Composing AND gates





# Translator gate (“wire”)

input X



We need a “wire” to translate the signal:

$X \rightarrow Y$

(with no shared DNA sequences between X and Y)

output Y



# Translator gate (a “wire”)

input X

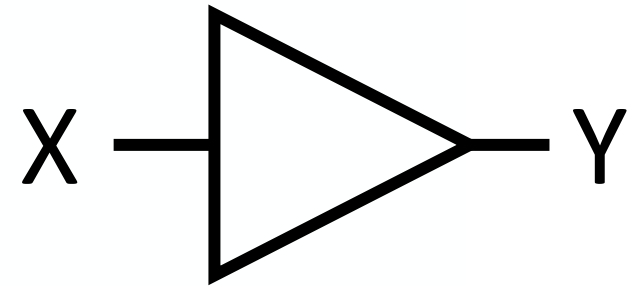


bind

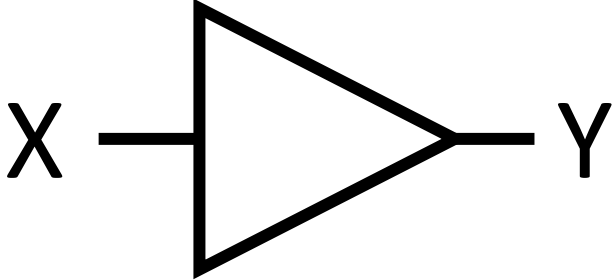
F<sub>1</sub>



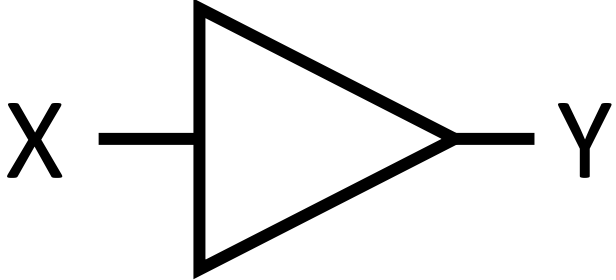
F<sub>2</sub>



# Translator gate (a “wire”)



# Translator gate (a “wire”)



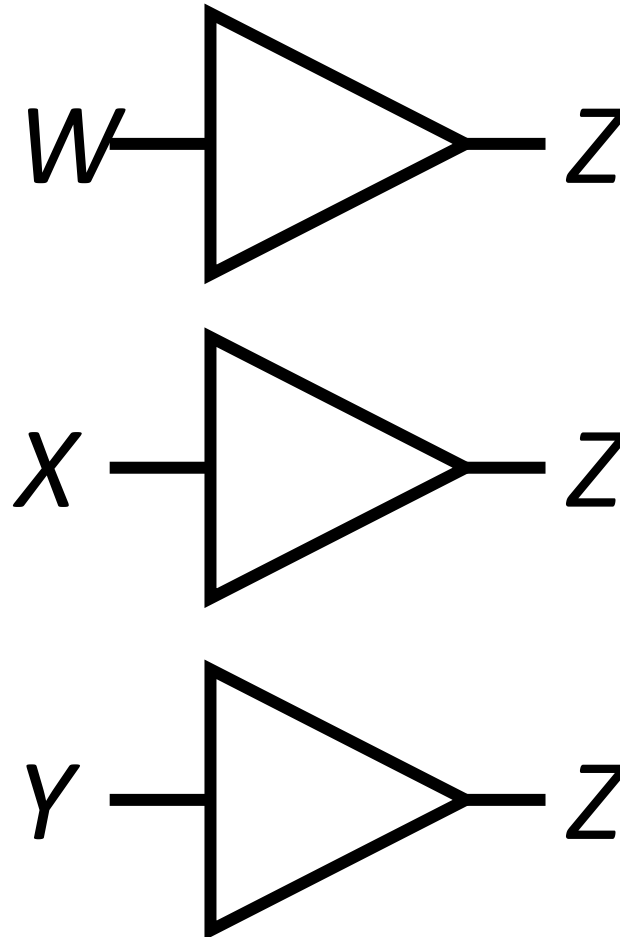
output Y



# Strand displacement cascade example: OR gate

An OR gate can be implemented by multiple translators:

$$Z \leftarrow W \text{ OR } X \text{ OR } Y$$

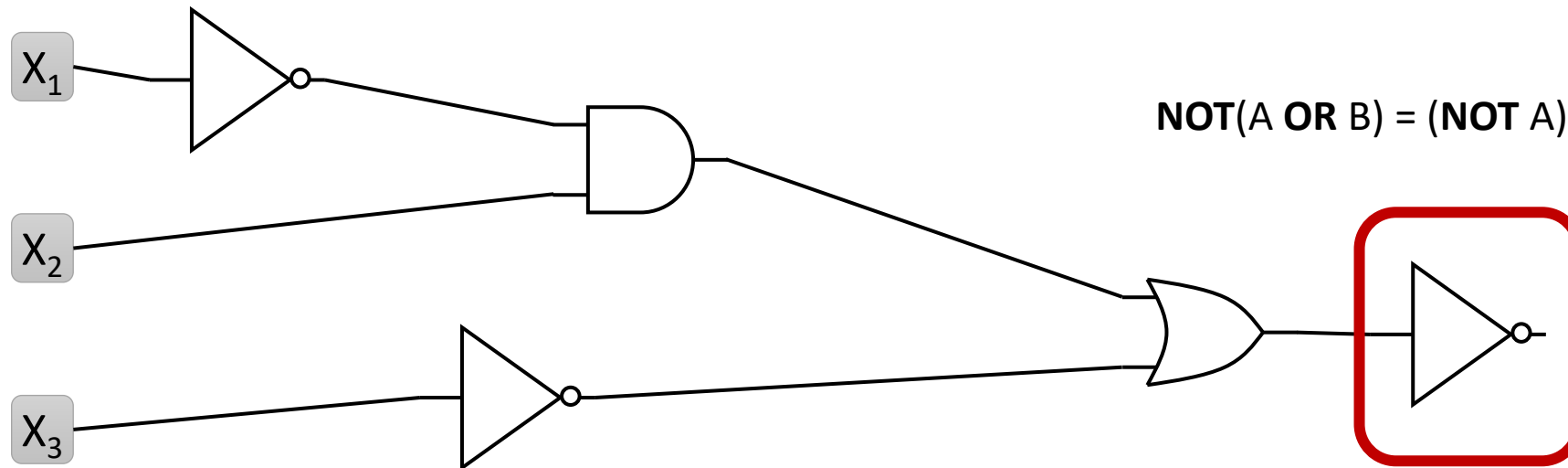


# Strand displacement cascade example: Avoiding the need for NOT gates using dual-rail logic

NOT gates are tricky with molecular circuits:  
How to make a molecule Y present  
if and only if X is not present??

Instead we use dual-rail logic, using de Morgan's  
Laws to push all the NOT gates to the input.

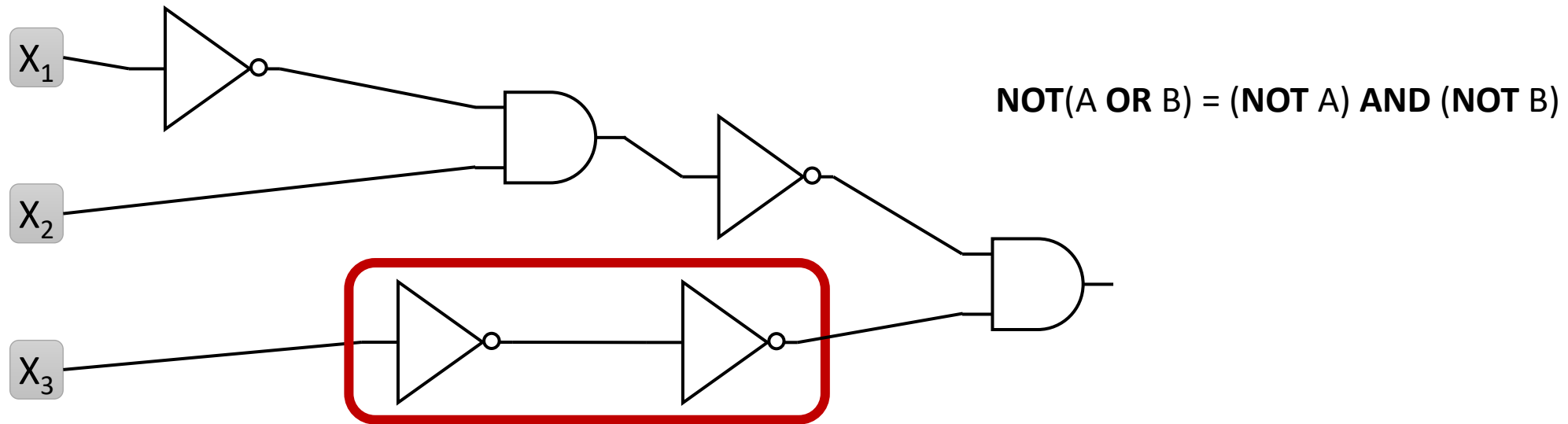
(Then we can "manually" specify FALSE input  
values by the presence of a "negated" strand.)



# Strand displacement cascade example: Avoiding the need for NOT gates using dual-rail logic

NOT gates are tricky with molecular circuits:  
How to make a molecule Y present  
if and only if X is not present??

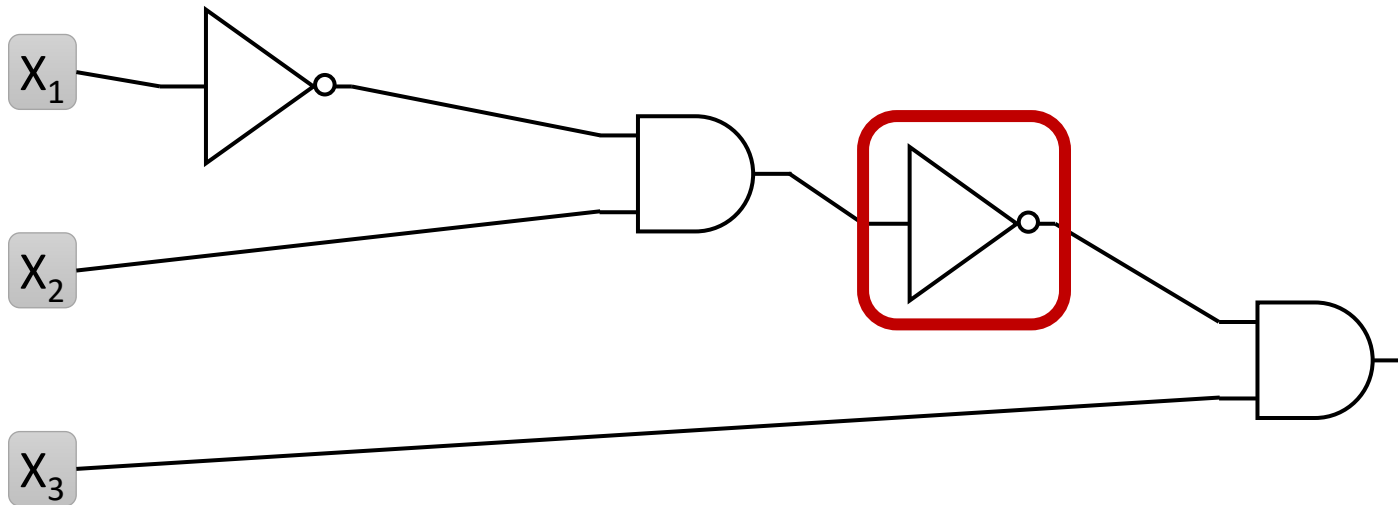
Instead we use “dual-rail” logic, using de Morgan’s Laws to push all the NOT gates to the input, so we can “manually” specify FALSE input values.



# Strand displacement cascade example: Avoiding the need for NOT gates using dual-rail logic

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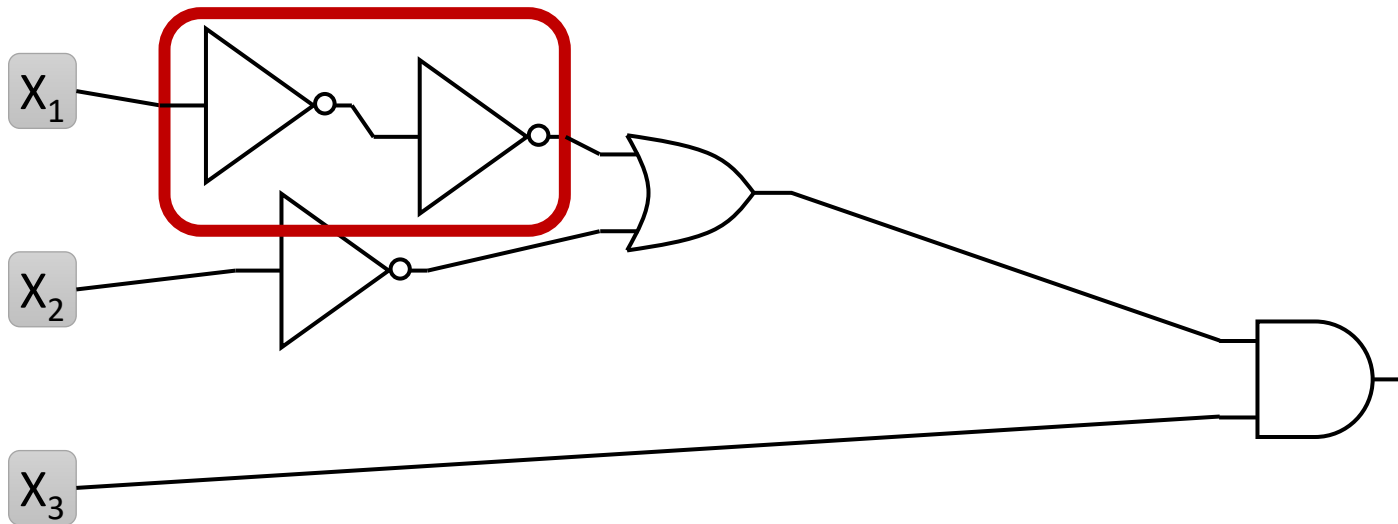




# Strand displacement cascade example: Avoiding the need for NOT gates using dual-rail logic

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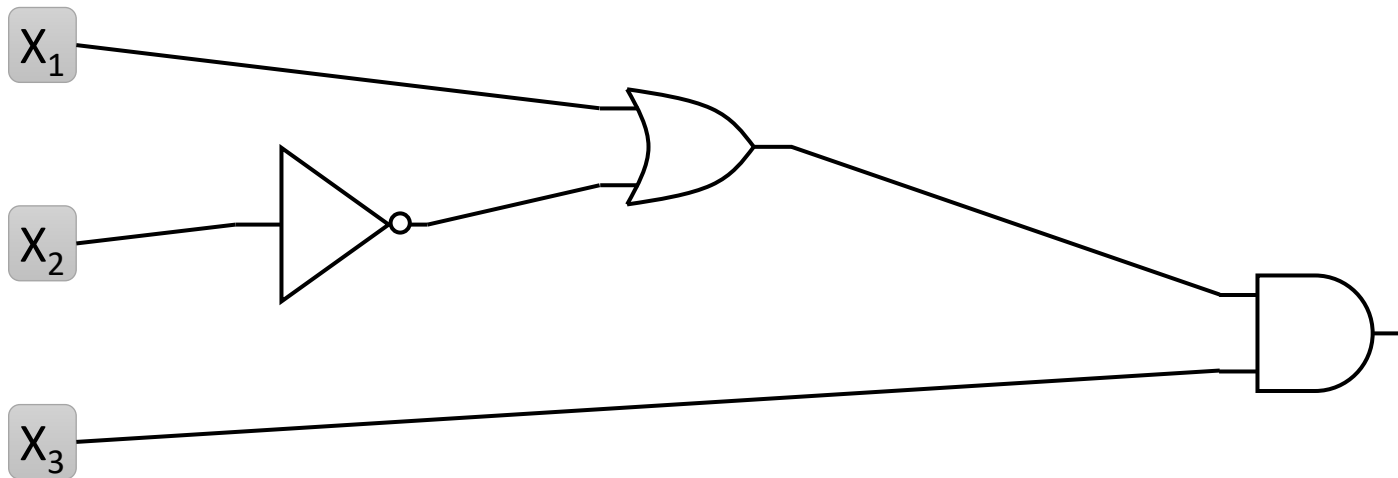
Instead we use “dual-rail” logic, using de Morgan’s Laws to push all the NOT gates to the input, so we can “manually” specify FALSE input values.



# Strand displacement cascade example: Avoiding the need for NOT gates using dual-rail logic

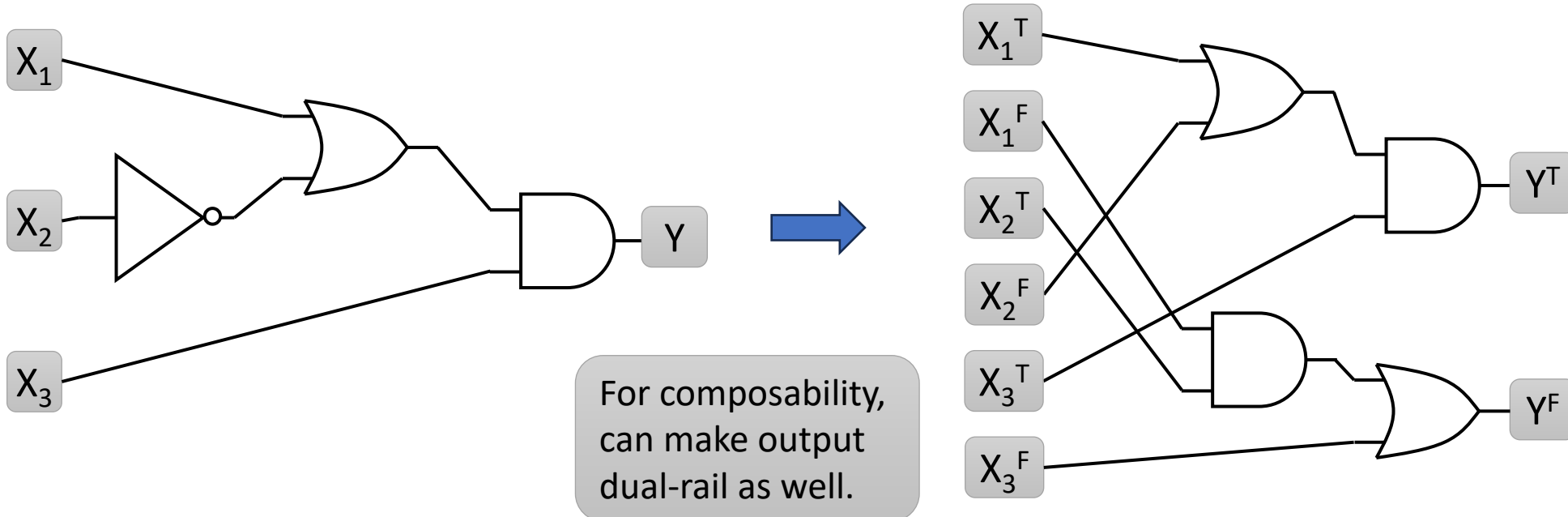
NOT gates are tricky with molecular circuits:  
How to make a molecule Y present  
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Instead we use “dual-rail” logic, using de Morgan’s Laws to push all the NOT gates to the input, so we can “manually” specify FALSE input values.

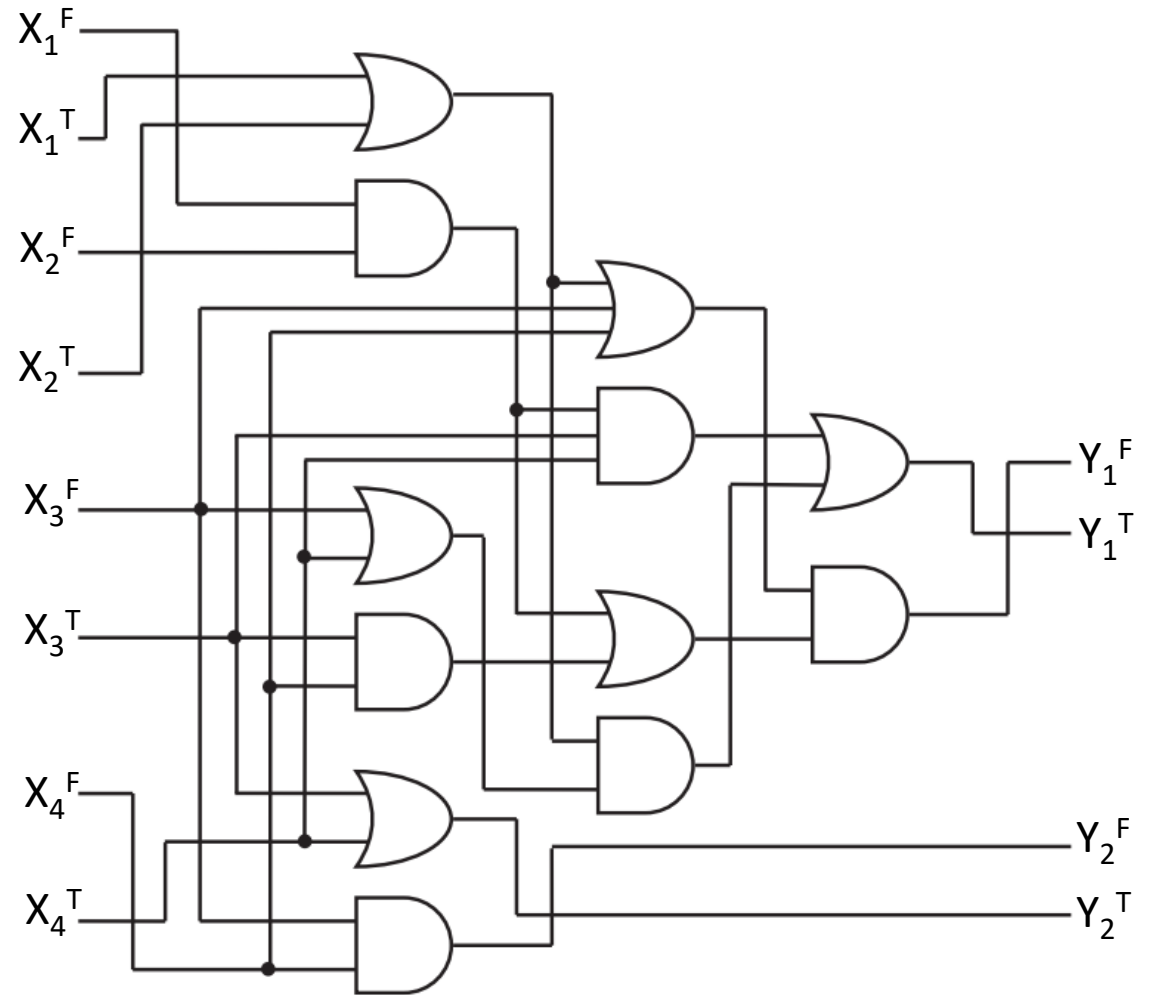
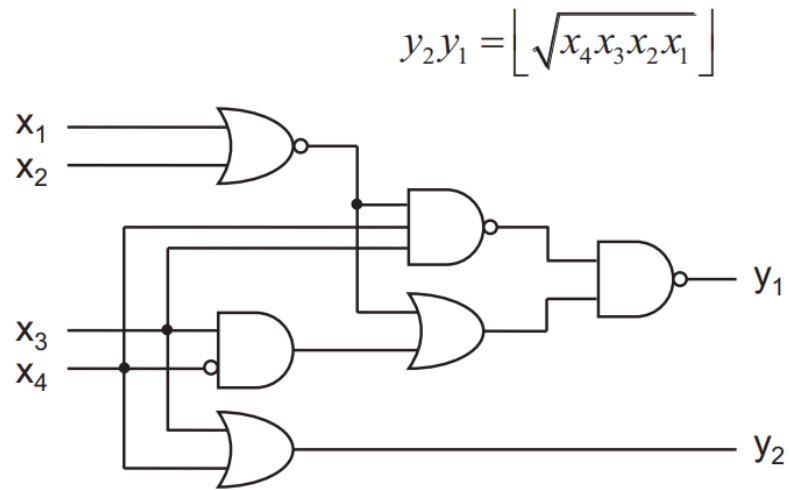


# Strand displacement cascade example: Avoiding the need for NOT gates using dual-rail logic

For each input  $X_i$ , there are two species  $X_i^T$  and  $X_i^F$ :  
Give species  $X_i^F$  to specify that Boolean input  $X_i = \textit{False}$   
Give species  $X_i^T$  to specify that Boolean input  $X_i = \textit{True}$ .



# Dual-rail logic computing square root of 4-bit number

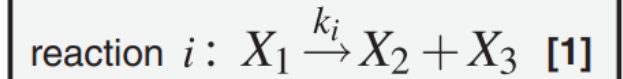
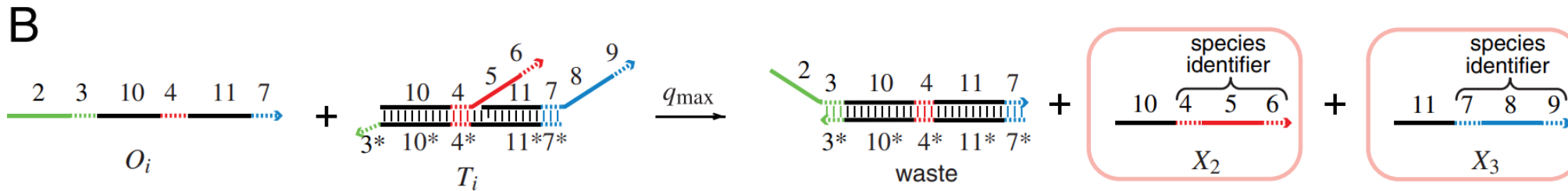
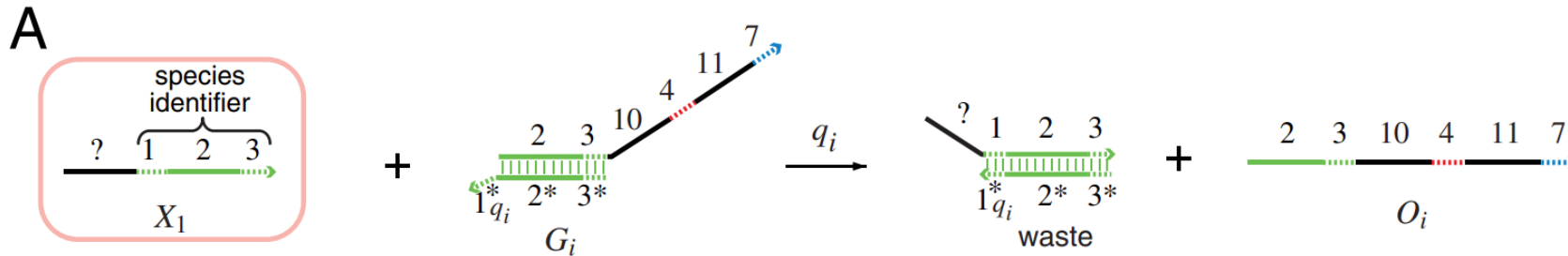


# Implementing CRNs with DNA

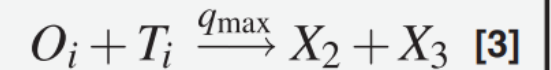
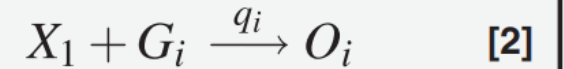
“Compiling” arbitrary chemical reaction networks into DNA strands that implement the reactions using DNA strand displacement

# DNA strand displacement can implement any CRN

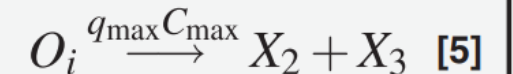
unimolecular reaction  $X_1 \rightarrow X_2 + X_3$



$\Downarrow$  implement

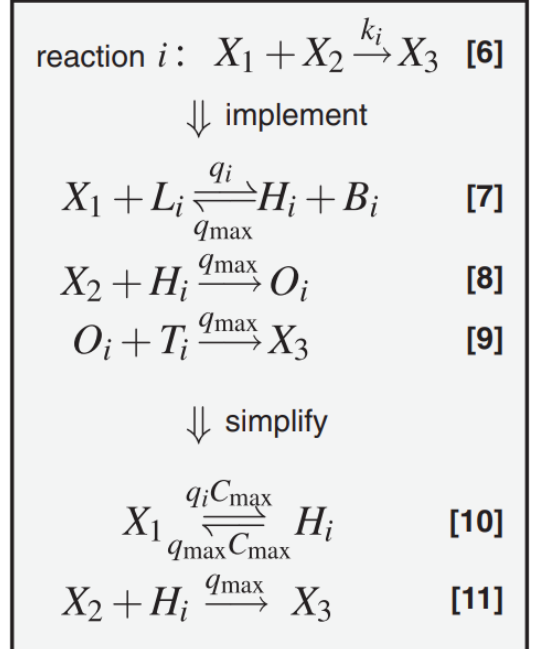
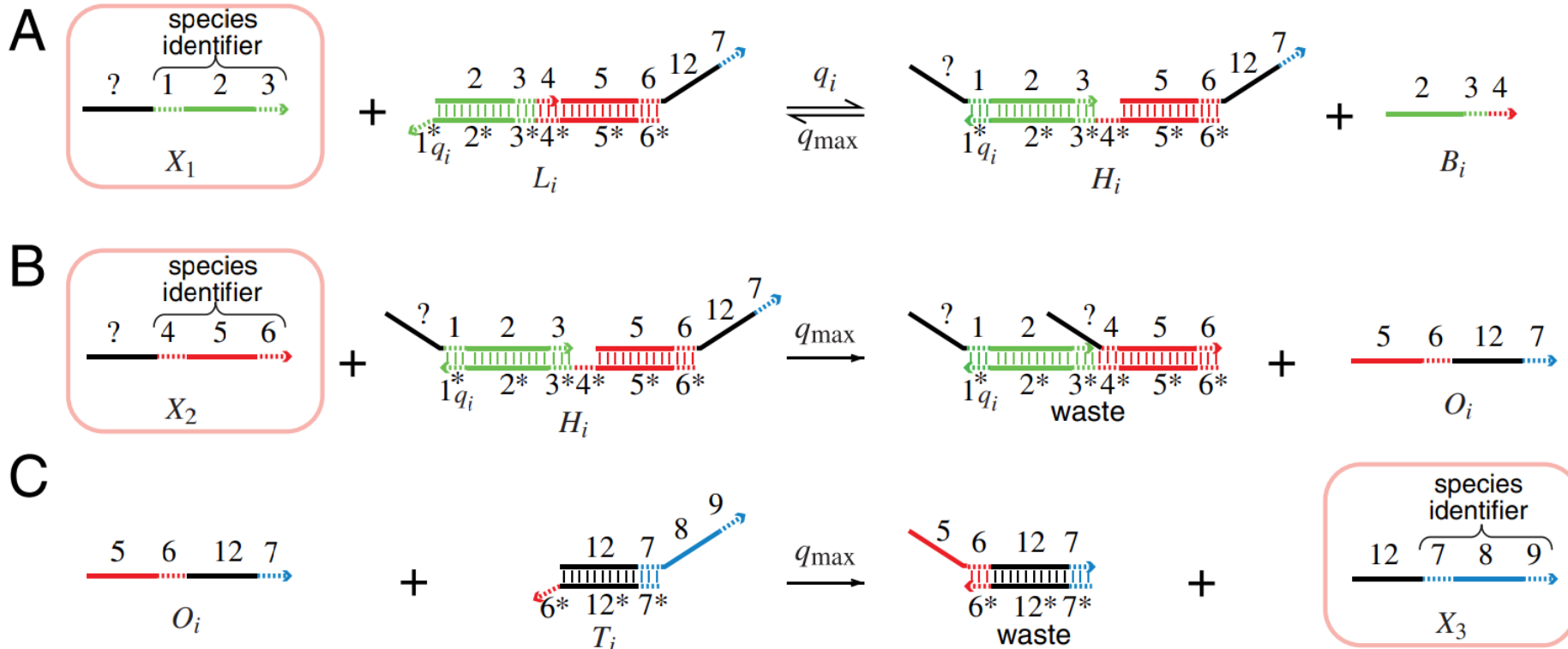


$\Downarrow$  simplify



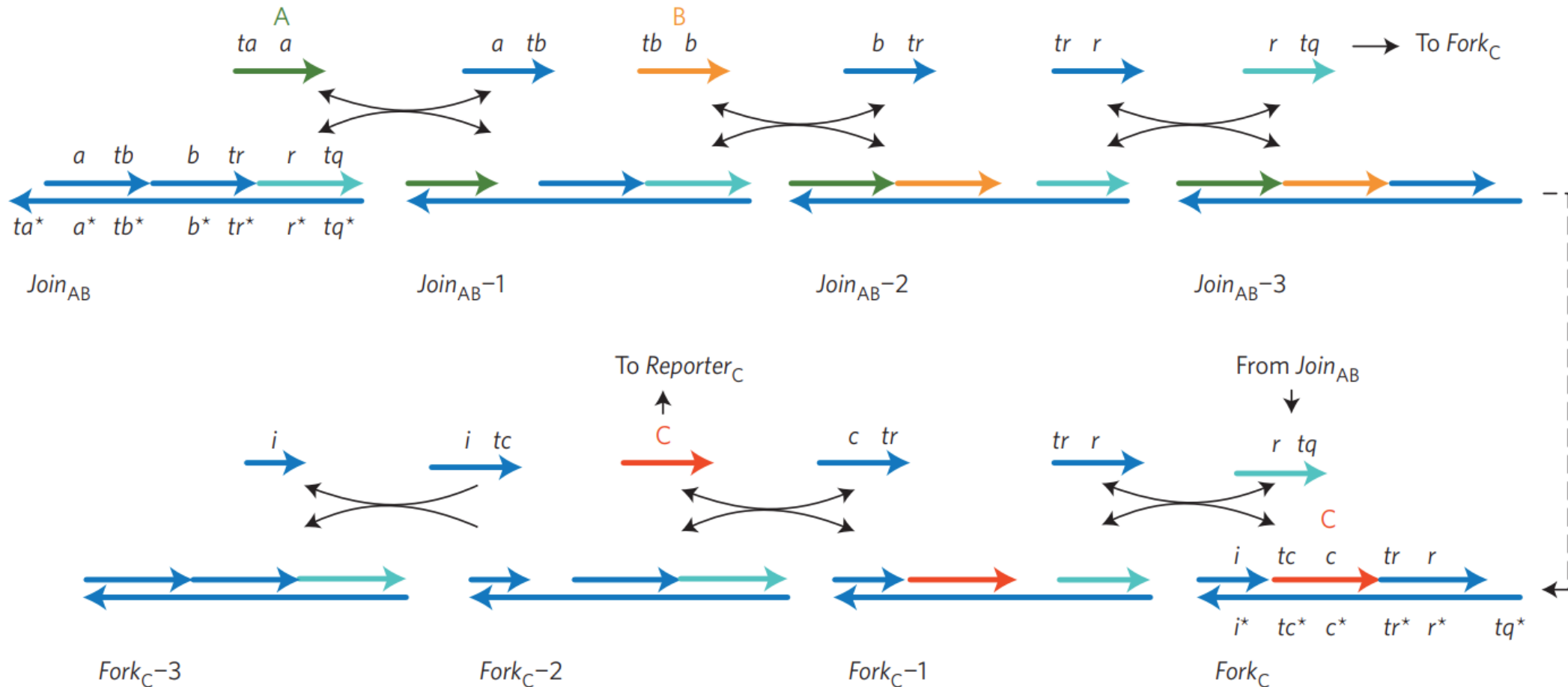
# DNA strand displacement can implement any CRN

bimolecular reaction  $X_1 + X_2 \rightarrow X_3$



# “Two-domain” scheme for compiling CRN to DSD

reaction  $A+B \rightarrow C$



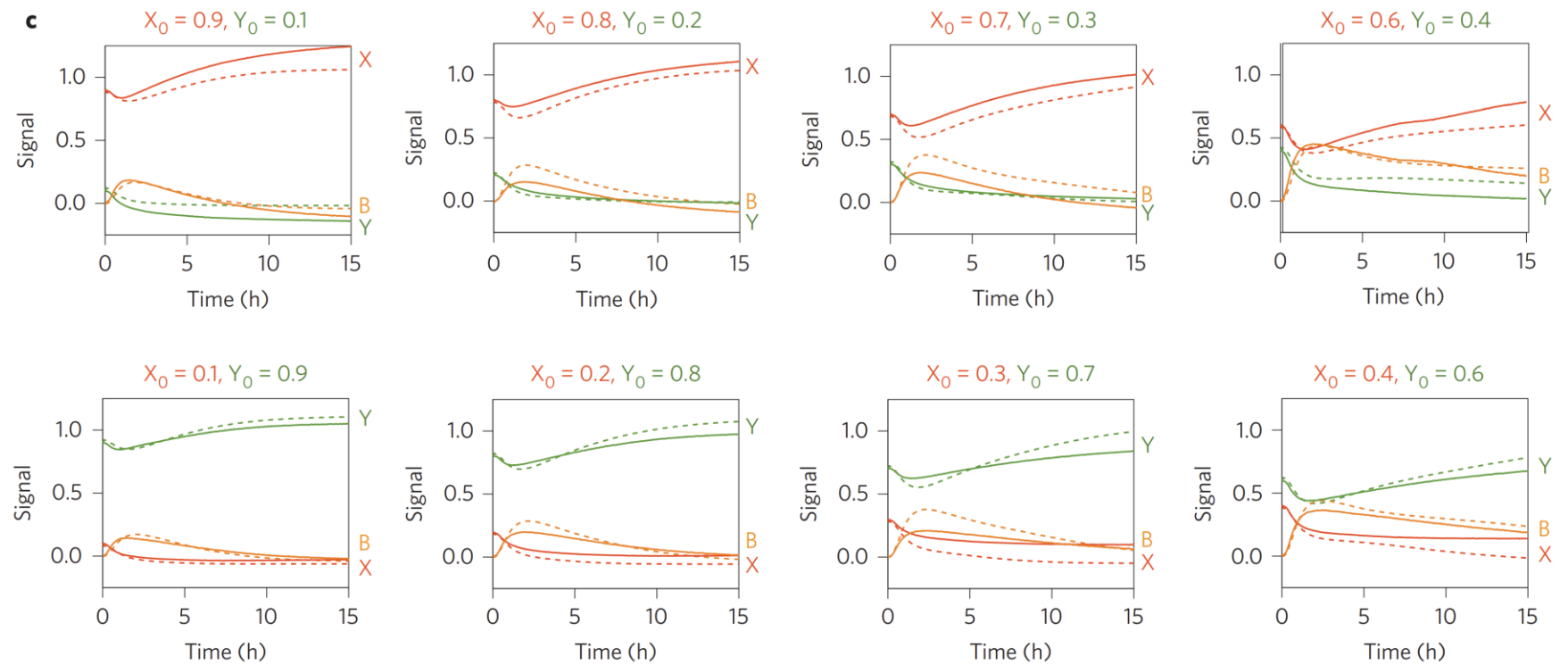
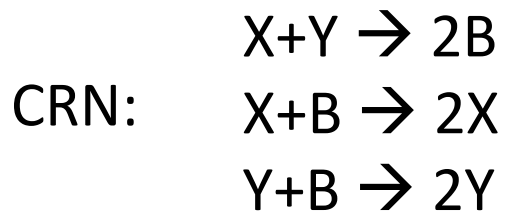
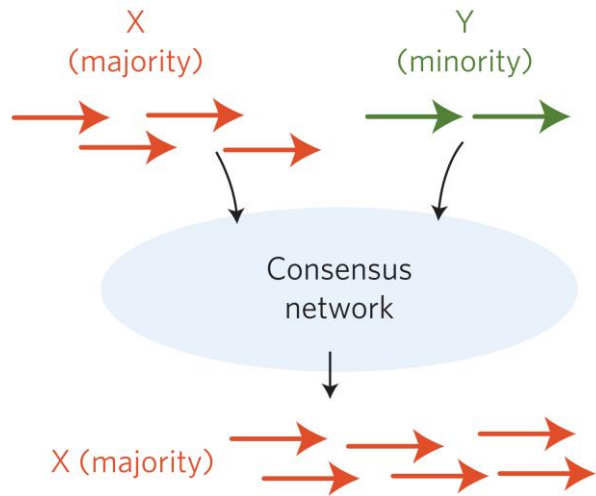
[Programmable chemical controllers made from DNA. Yuan-Jyue Chen, Neil Dalchau, Niranjan Srinivas, Andrew Phillips, Luca Cardelli, David Soloveichik, and Georg Seelig. *Nature Nanotechnology* 2013.]



# Experimental implementations of CRN-to-DSD schemes

# DSD computing approximate majority

Goal:



# DSD implementing chemical “rock-paper-scissors” oscillator

