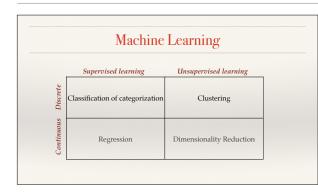
Neural Networks	Supervised learning	

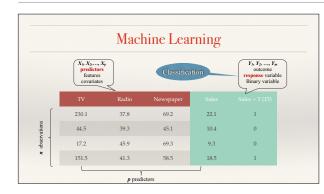






		Machine	Learning	
	X ₁ , X ₂ ,, X _p predictors features covariates			Y ₁ , Y ₂ ,, Y _m outcome response variable Continuous variable
	TV	Radio	Newspaper	Sales
ſ	230.1	37.8	69.2	22.1
vations	44.5	39.3	45.1	10.4
n observations	17.2	45.9	69.3	9.3
=	151.5	41.3	58.5	18.5

]	Machine	Learning	
	X ₁ , X ₂ ,, X _p predictors features covariates	•	Regression	Y ₁ , Y ₂ ,, Y _m outcome response variable Continuous variable
	TV	Radio	Newspaper	Sales
ſ	230.1	37.8	69.2	22.1
	44.5	39.3	45.1	10.4
1 0020140100	17.2	45.9	69.3	9.3
	151.5	41.3	58.5	18.5



Statistical Model We assume that the response variable, Y, relates to the predictors, X, through some unknown function expressed generally as: Y = f(X) + b Here, f is the unknown function expressing an underlying rule for relating Y to X, b is the amount (unrelated to X) that Y differs from the rule f(X). A statistical model is any algorithm that estimates f. We denote the estimated function as \hat{f} .

Statistical Model

We assume that the response variable, Y, relates to the predictors, X, through some unknown function expressed generally as:

Y = f(X) + b

The question is then, how well do we want to know f/\hat{f} ?

- We want to understand the mechanism underlying the data: in this case we really need to find the "correct" expression for *f*.

- We only want to use \hat{f} to predict the response for yet unknown predictor values: we may not need a correct expression for f_r as long as the prediction is correct!

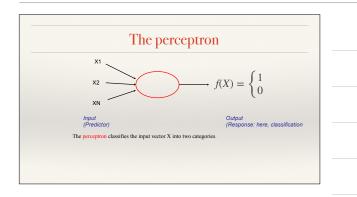
Statistical Model

We assume that the response variable, Y, relates to the predictors, X, through some unknown function expressed generally as:

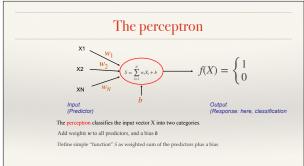
Y = f(X) + b

Building a model, non necessarily realistic, for *f*: - Try polynomial function - Try any mathematical function

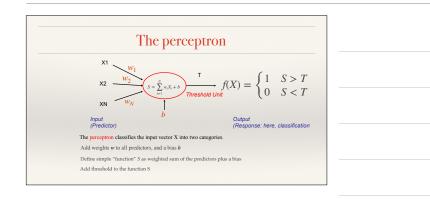


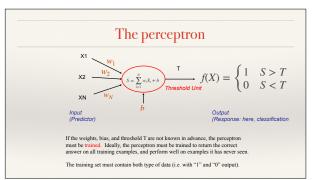




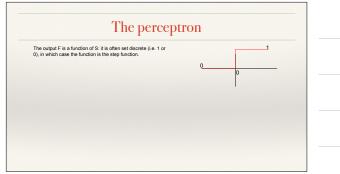






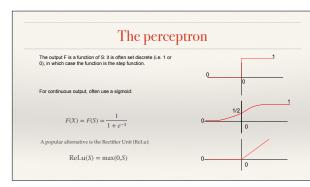




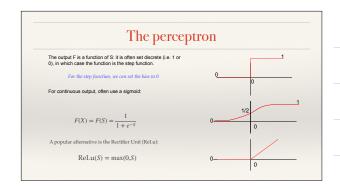






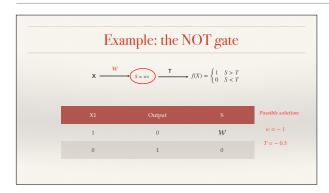




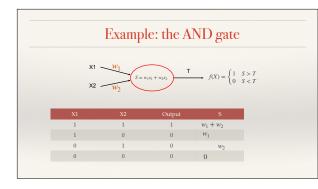


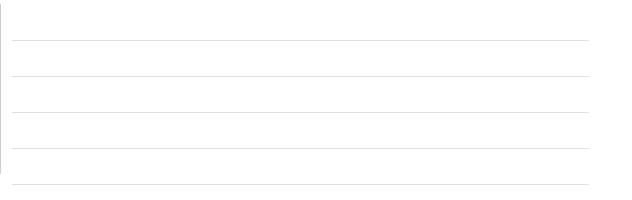




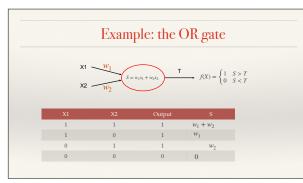




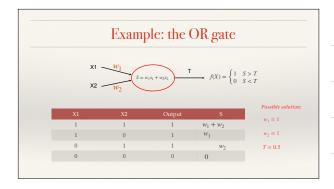




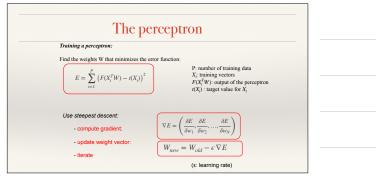




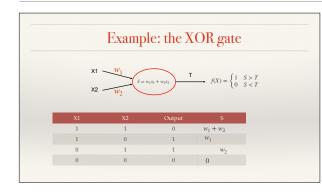




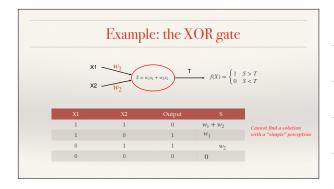




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ne perceptron r X _i		
]	

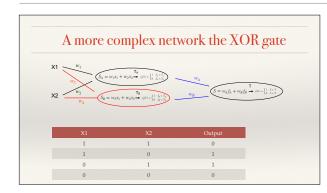


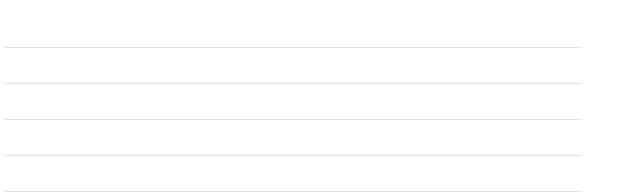






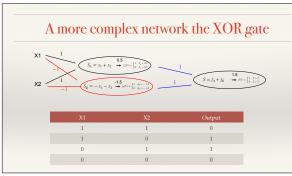
TA	vork the XC	
N . (m. [1 5>T]		
$1_2X_2 \rightarrow \ell_0 X) = \begin{cases} 1 & S > T_1 \\ 0 & S < T_2 \end{cases}$		
$W_{4}X_{2} \rightarrow f_{4}(X) = \begin{cases} 1 & S > T_{4} \\ 0 & S < T_{6} \end{cases}$		
X2	Output	
1	0	
0	1	
1	1	
0	0	
	$\begin{array}{c} \mathbf{T}_{\mathbf{r}} \\ \mathbf{w}_{\mathbf{z}} \mathbf{x}_{2} \rightarrow \boldsymbol{\omega}_{\mathbf{r}} \in \left\{ \begin{array}{c} \mathbf{z} \neq \mathbf{z} \\ \mathbf{z} \neq \mathbf{z} \\ \mathbf{z} \\$	X2 Output 1 0 0 1 1 1





A m	ore c	omple	x netv	vork t	he XOR	oate
11 11		ompic	Anety	VOIKU	ne non	gaic
X1		TA	_			
w3	$S_A = w_1$	$x_1 + w_2 x_2 \rightarrow f(x) =$	$\begin{cases} 1 & S_k > T_k \\ 0 & S_k < T_k \end{cases}$	WA	T	_
X2	$S_B = w$	T_{B} $v_{3}x_{1} + w_{4}x_{2} \rightarrow f_{0}(x)$	$= \begin{cases} 1 & S_0 > T_0 \\ 0 & S_0 < T_0 \end{cases}$	w _B	$S = w_A f_A + w_B f_B \rightarrow \infty$	$X = \begin{cases} 1 & S > T \\ 0 & S < T \end{cases}$
W2						
		"Hidden layer"			"Output la	tyer
_						
X1	X2	Output	S_A	S_B	S	
X1 1	X2 1	Output 0	S_A $w_1 + w_2$	$S_B = w_1 + w_2$	S $w_A f_A + w_B f_B$	
X1 1 1	X2 1 0					
1	1	0	$w_1 + w_2$	$w_1 + w_2$	$w_A f_A + w_B f_B$	





OR gate	
$1.5 \qquad \qquad$	
-	



