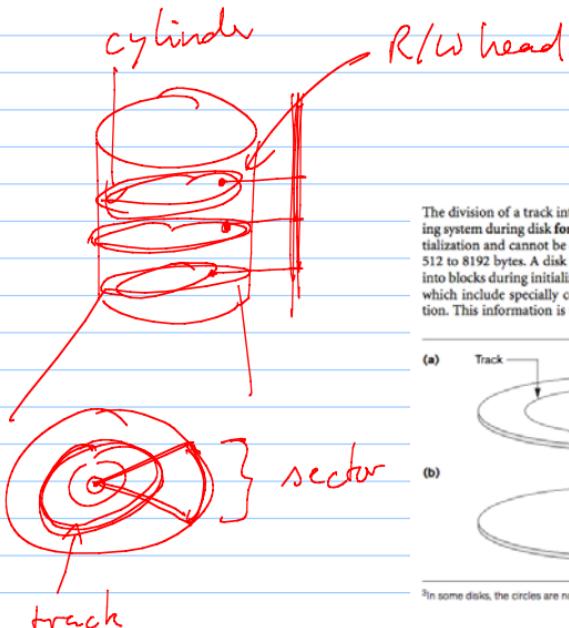
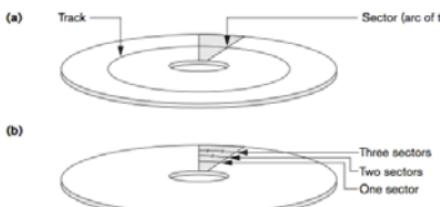
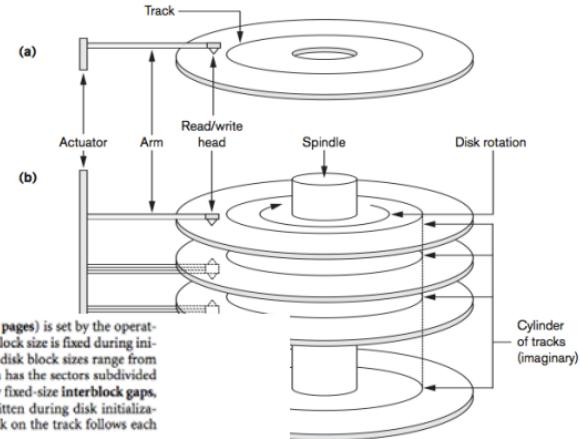


6. Storage

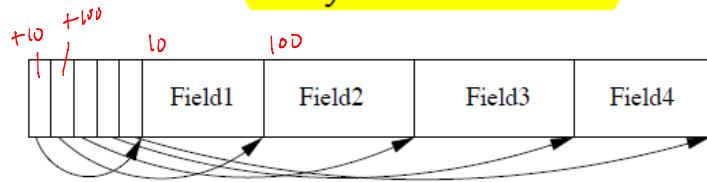


The division of a track into equal-sized disk **blocks** (or pages) is set by the operating system during disk **formatting** (or **initialization**). Block size is fixed during initialization and cannot be changed dynamically. Typical disk block sizes range from 512 to 8192 bytes. A disk with hard-coded sectors often has the sectors subdivided into blocks during initialization. Blocks are separated by fixed-size **interblock gaps**, which include specially coded control information written during disk initialization. This information is used to determine which block on the track follows each



?In some disks, the circles are now connected into a kind of continuous spiral.

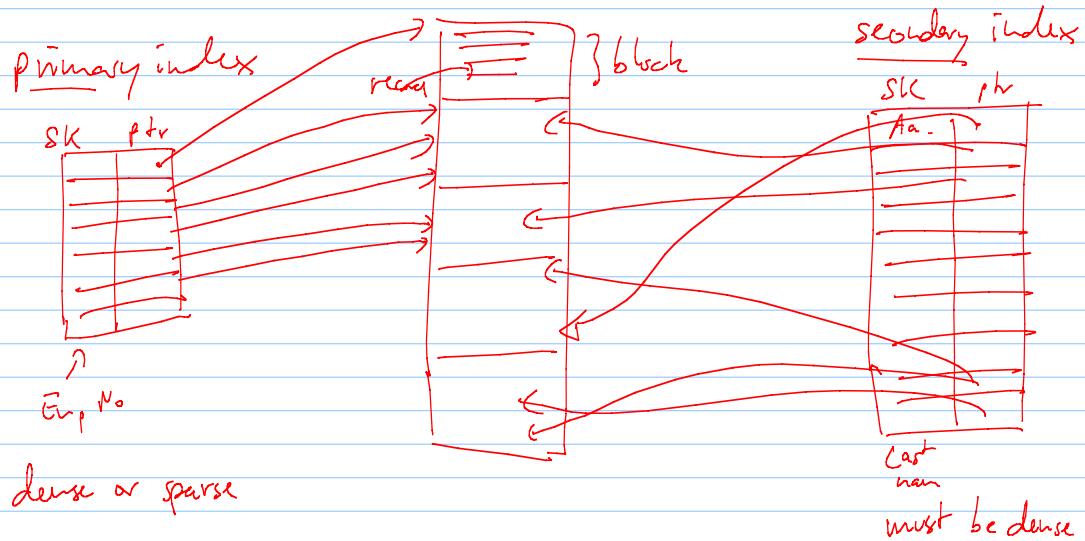
3. Each record has an **array of field offsets**

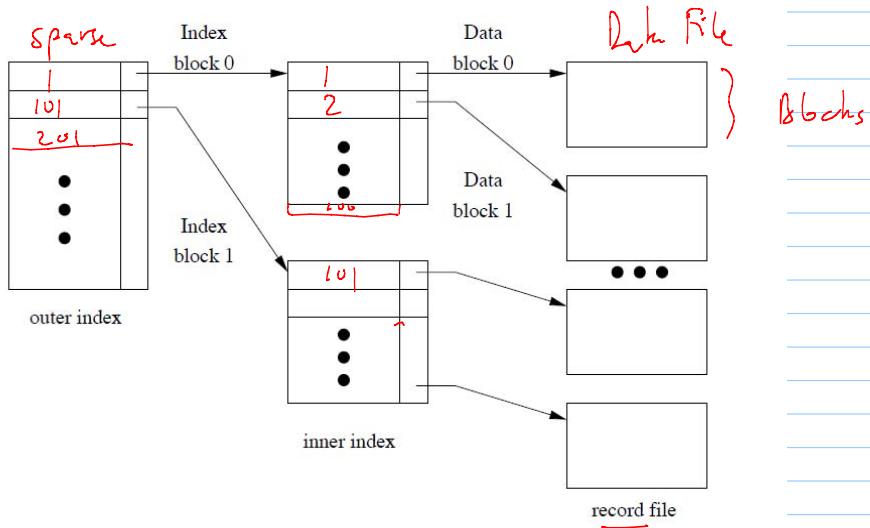


- + For the overhead of the offset, we get direct access to any field
- + Null values: begin/end pointer of a field point to the same address

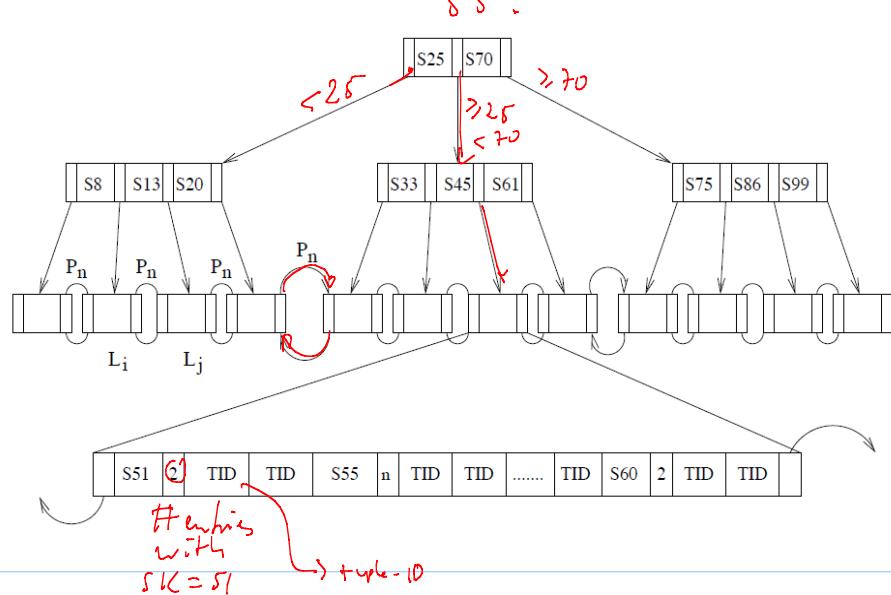
7. Indexing

EMPLOYEE file (sorted by Emp No)





Example of a B⁺-Tree

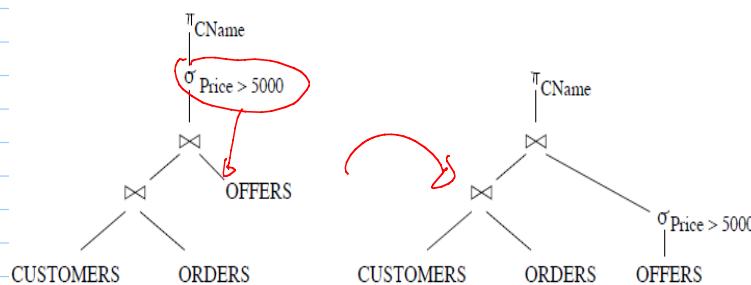


9. Query Processing

$$\pi_{\text{CName}}(\sigma_{\text{Price} > 5000}((\text{CUSTOMERS} \bowtie \text{ORDERS}) \bowtie \text{OFFERS}))$$

$$\pi_{\text{CName}}((\text{CUSTOMERS} \bowtie \text{ORDERS}) \bowtie (\sigma_{\text{Price} > 5000}(\text{OFFERS})))$$

Representation as *logical query plan* (a tree):



$$(A \bowtie B) \bowtie C$$

$$= A \bowtie (B \bowtie C)$$

- N_R : number of tuples in the relation R.
- B_R : number of blocks that contain tuples of the relation R.
- S_R : size of a tuple of R.
- F_R : blocking factor; number of tuples from R that fit into one block ($F_R = \lceil N_R / B_R \rceil$)
- $V(A, R)$: number of distinct values for attribute A in R.
- $SC(A, R)$: selectivity of attribute A
≡ average number of tuples of R that satisfy an equality condition on A. $\sim \sigma_{A=c}(R)$

$$SC(A, R) = N_R / V(A, R).$$

$$1 \dots N_R$$

$$|T_A(R)|$$

if A is a key $\wedge V(A, R) = N_R$

→ big value for V $\sim SC \sim 1$
 \Rightarrow very selective

→ small value for V $\sim SC \sim N_R$
 \Rightarrow not selective

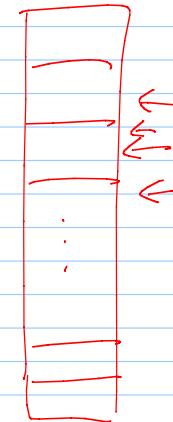
- **S2 – Binary search**, i.e., the file ordered based on attribute A (primary index)

$$\text{cost}(S2) = \lceil \log_2(B_R) \rceil + \left\lceil \frac{SC(A, R)}{F_R} \right\rceil - 1$$

block with result tuples

- $\lceil \log_2(B_R) \rceil \equiv$ cost to locate the first tuple using binary search ✓
- Second term \equiv blocks that contain records satisfying the selection. ✓
- If A is primary key, then $SC(A, R) = 1$, hence $\text{cost}(S2) = \lceil \log_2(B_R) \rceil$.

sorted
 $G_{A=\leq}(R)$



- **Example (for Employee DB)**

– $F_{Employee} = 10$;
 $V(\text{Deptno, Employee}) = 50$ (different departments)

$\hookrightarrow \Pi_{\text{Deptno}}(Employee)$

– $N_{Employee} = 10,000$ (Relation Employee has 10,000 tuples)

– Assume selection $\sigma_{\text{Deptno}=20}(\text{Employee})$ and Employee is sorted on search key Deptno :

$N_R \propto O(\log n)$

$\Rightarrow 10,000/50 = 200$ tuples in Employee belong to Deptno 20;

(assuming an equal distribution)

$200/10 = 20$ blocks for these tuples

\Rightarrow A binary search finding the first block would require $\lceil \log_2(1,000) \rceil = 10$ block accesses $\beta \leftarrow$ free

Total cost of binary search is $10+20$ block accesses (versus 1,000 for linear search and Employee not sorted by Deptno).

blocks with dept=20 employees

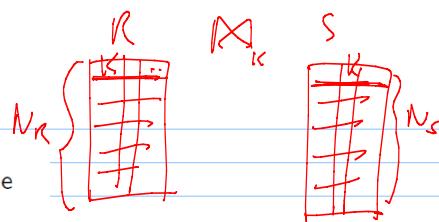
Complex Selections

- General pattern:
 - Conjunction – $\sigma_{\theta_1 \wedge \dots \wedge \theta_n}(R)$
 - Disjunction – $\sigma_{\theta_1 \vee \dots \vee \theta_n}(R)$
 - Negation – $\sigma_{\neg \theta}(R)$

$$p(\theta_1) \cdot p(\theta_2)$$

$$p(\theta_1) + p(\theta_2) - p(\theta_1 \wedge \theta_2)$$

$R \bowtie S$



- If $\text{schema}(R) \cap \text{schema}(S) = \text{primary key}$ for R, then a tuple of S will match with at most one tuple from R.
Therefore, the number of tuples in $R \bowtie S$ is not greater than $\underline{N_S} \geq |R \bowtie S|$

If $\text{schema}(R) \cap \text{schema}(S) = \text{foreign key in } S \text{ referencing } R$, then the number of tuples in $R \bowtie S$ is exactly N_S .

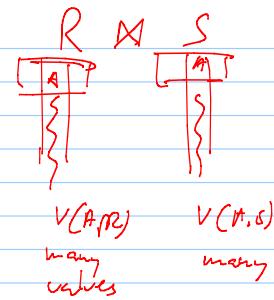
Other cases are symmetric.

- In the example query CUSTOMERS \bowtie ORDERS, CName in ORDERS is a foreign key of CUSTOMERS; the result thus has exactly $N_{ORDERS} = 10,000$ tuples

- If $\text{schema}(R) \cap \text{schema}(S) = \{A\}$ is not a key for R or S; assume that every tuple in R produces tuples in $R \bowtie S$. Then the number of tuples in $R \bowtie S$ is estimated to be:

$$\frac{N_R * N_S}{V(A, R)}$$

$$= SC(A, S)$$



If the reverse is true, the estimate is $\frac{N_R * N_S}{V(A, S)} = SC(A, R)$

and the lower of the two estimates is probably the more accurate one.

- Evaluate the condition join $R \bowtie_C S$
- **for each tuple t_R in R do begin**
for each tuple t_S in S do begin
 check whether pair (t_R, t_S) satisfies join condition
 if they do, add $t_R \circ t_S$ to the result
end
end
- R is called the **outer** and S the **inner** relation of the join.
- Requires no indexes and can be used with any kind of join condition.
- **Worst case:** db buffer can only hold one block of each relation
 $\Rightarrow B_R + N_R * B_S$ disk accesses
- **Best case:** both relations fit into db buffer
 $\Rightarrow B_R + B_S$ disk accesses.

