

Quiz 1

1. List, in lexicographic order, the first five strings of $\{aa, b\}^*$.
2. Draw a smallest DFA that accepts $L = \{x \in \{0, 1\}^* : \text{the number that } x \text{ represents, in binary, is divisible by 3}\} = \{0\}^*\{\varepsilon, 11, 110, 1001, \dots\}$. (smallest = fewest states)
3. Draw a smallest NFA for the language $L = \{01, 001\}$.
4. Every NFA-acceptable language can be accepted by an NFA with just a single final state.
5. L^* is infinite.
6. $(L^*)^* = L^*$.
7. If $M = (Q, \Sigma, \delta, q_0, F)$ is a DFA and $F = Q$ then $L(M) = \Sigma^*$.
8. If L is accepted by an n -state NFA then L is accepted by some $2 + 2^n$ -state DFA.
9. If L is DFA-acceptable and F is finite then $L \cap F$ is a DFA-acceptable.
10. Let $M = (Q, \{0, 1\}, \delta, q_0, F)$ be a DFA and suppose that $\delta^*(q_0, x) = \delta^*(q_0, y)$. Let $z \in \{0, 1\}^*$. Then $xz \in L(M)$ iff $yz \in L(M)$.